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**DEMOSTRACIÓN DEL ESPECTRO
HAMILTONIANO PARA UN CAMPO DE YANG-
MILLS NO ABELIANO QUE POSEEN UNA
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ESTADO DE VACÍO**

**DEMONSTRATION OF THE HAMILTONIAN SPECTRUM FOR A
NON-ABELIAN YANG-MILLS FIELD POSSESSING A FINITE
MASS GAP WITH RESPECT TO THE VACUUM STATE**

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Demostración del Espectro Hamiltoniano para un Campo de Yang-Mills no Abeliano que Poseen una Brecha de Masa Finita con Respecto al Estado de Vacío

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RESUMEN

El presente artículo científico, tiene como propósito, demostrar, a través de la conjugación estructurada de distintos componentes interaccionados, que conforman el sistema de campos de Yang-Mills, **(i)** la conjetura de que las excitaciones más bajas de una teoría pura de Yang-Mills (es decir, sin campos de materia) tienen una brecha de masa finita con respecto al estado de vacío; **(ii)** la propiedad de confinamiento en presencia de partículas adicionales; y, **(iii)** que, dado un *hamiltoniano cuántico* para un campo de Yang-Mills no abeliano, existe un valor positivo mínimo de la energía. La solución de los problemas antes descritos, requiere tanto la comprensión de uno de los profundos misterios de la física sin resolver, esto es, la existencia de una brecha de masa, como la producción de un ejemplo matemáticamente completo de la teoría cuántica de campos gauge en el espacio-tiempo de cuatro dimensiones, lo que se aborda rigurosamente en el presente artículo científico.

Palabras clave: física cuántica, escala subatómica, campos de yang-mills, teorías de gauge, brecha de masa

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Demonstration of the Hamiltonian Spectrum for a Non-Abelian Yang-Mills Field Possessing a Finite Mass Gap With Respect to the Vacuum State

ABSTRACT

The purpose of this scientific article is to demonstrate, through the structured conjugation of different interacted components that make up the Yang-Mills field system, **(i)** the conjecture that the lowest excitations of a pure Yang-Mills theory (i.e., without matter fields) have a finite mass gap with respect to the vacuum state; **(ii)** the property of confinement in the presence of additional particles; and, **(iii)** that, given a quantum Hamiltonian for a non-abelian Yang-Mills field, there is a minimum positive value of energy. The solution of the problems described above requires both the understanding of one of the profound unsolved mysteries of physics, that is, the existence of a mass gap, and the production of a mathematically complete example of the quantum theory of gauge fields in four-dimensional spacetime, which is rigorously addressed in the present work.

Keywords: quantum physics, subatomic scale, yang-mills fields, gauge theories, mass gap

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INTRODUCCIÓN

Ciertamente, la descripción de la naturaleza a escala subatómica requiere de la física cuántica. En la física cuántica, la posición y la velocidad de una partícula se tienen como operadores no conmutadores que interactúan en un espacio de Hilbert. Es así, donde muchos aspectos de la naturaleza se describen en forma de campos. Dado que los campos interactúan con las partículas, deviene en indispensable, incorporar conceptos cuánticos tanto para describir campos como para describir partículas. En los campos convencionales, existe una partícula y por regla general, una antipartícula, con la misma masa y carga, pero opuesta, verbigracia, el campo cuantizado de los electrones.

Siguiendo este mismo orden de cosas, se tiene que, las teorías de gauge (teorías cuánticas de campos [QFT]), es una de las más importantes en cuanto a física de partículas se refiere. Un ejemplo claro de ello, es la teoría del electromagnetismo de Maxwell que comporta un grupo de simetría gauge en un grupo abeliano $U(1)$. Sin embargo, la teoría de Yang – Mills, en este contexto, califica una teoría gauge no abeliana.

La ecuación clásica y variacional central del lagrangiano Yang-Mills, se escribe así:

$$L = \frac{1}{4g^2} \int \text{Tr } F \wedge *F,$$

donde Tr denota una forma cuadrática invariante en el álgebra de Lie de G . Las ecuaciones de Yang-Mills no son lineales, por lo que, no existen soluciones exactas de la ecuación clásica antes referida, y es lo que se propone resolver este trabajo a través de un riguroso cálculo matemático, desde la óptica del hamiltoniano cuántico. En consecuencia, este trabajo, pretende demostrar, que la teoría gauge no abeliana de Yang – Mills, describe otras fuerzas en la naturaleza, especialmente la fuerza débil (responsable, entre otras cosas, de ciertas formas de radiactividad) y la fuerza fuerte o nuclear (responsable, entre otras cosas, de la unión de protones y neutrones en núcleos), pero sin perder las premisas esenciales de la teoría de campos de Yang – Mills, esto es, por fuera de la teoría electrodébil de Glashow-Salam-Weinberg o la teoría del “campo de Higgs”.



Si bien es cierto, constituyese en una propiedad notable de la teoría cuántica de Yang-Mills, la nominada "libertad asintótica", la misma que supone, que a distancias cortas, el campo muestra un comportamiento cuántico muy similar a su comportamiento clásico; sin embargo, a largas distancias, la teoría de Yang – Mills, fracasa en la descripción del campo. Otros componentes paralelos, que se abordan y resuelven en el presente trabajo, refieren a que: **(i)** existe una "brecha de masa" $\Delta >$ constante, tal que cada excitación del vacío tiene energía de al menos Δ ; **(ii)** existe un confinamiento de quarks, partiendo de la premisa de que, los estados físicos de las partículas, como el protón, el neutrón y el pión, son invariantes en SU(3); y, **(iii)** existe una "ruptura de simetría quiral", lo que significa que el vacío es potencialmente invariante solo bajo un cierto subgrupo de simetría completa que actúa sobre los campos de quarks.

METODOLOGÍA

El enfoque es cualitativo. El tipo de investigación es predictivo. El diseño utilizado es constructivista. No existe población de estudio toda vez que el presente artículo científico no es de carácter sociológico o social. Tampoco se han implementado técnicas de recolección de información tales como encuestas, etc, salvo revisión bibliográfica. Finalmente, el material de apoyo es meramente bibliográfico.

RESULTADOS Y DISCUSIÓN

Marco Praxeológico

a. Formulación matemática primaria (línea base):

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \mathcal{L}_{gf} = -1/2 \text{tr} (F_{\nu\rho}^{\mu\sigma}) = 1/4 F^{\alpha\mu\nu} F_{\alpha\mu\nu} F_{\mu\nu}^{\alpha} F_{\mu\nu}^{\alpha} F^c F_c$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \mathcal{L}_{fg} = -1/2 \text{tr} (F_{\mu\sigma}^{\nu\rho}) = 1/4 F^{\nu\mu b} F_{\nu\mu b} F_b^{\mu\nu} F_{\mu\nu}^b F^c F_c$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \text{tr}(T^a T_b T^a T_b) = 1\delta_b^a, [T^a T_b T^a T_b] = i f^{abc} f_{abc} T^c T_c$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \text{tr}(T^b T_a T^b T_a) = 1\delta_a^b, [T^b T_a T^b T_a] = i f^{abc} f_{abc} T^c T_c$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \text{tr}(T^a T_b T^b T_a) = 1\delta_{ba}^{ab}, [T^b T_a T^b T_a] = i f^{abc} f_{abc} T^c T_c$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle D_\mu = I\partial_\mu - ig T^a A_\nu^\mu, D_\nu = I\partial_\nu - ig T^b A_\mu^\nu$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\mu\nu}^a = \partial_\mu A_\nu^a - \partial_\nu A_\mu^a + g f^{abc} f_{abc} A_\mu^b A_\nu^c$$



Vértice de gluón -3:

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \Gamma_{\mu\nu\lambda}^{abc} \Gamma_{\nu\mu\lambda}^{abc}(p, q, r) = gf^{abc} gf_{abc} [(p - q)^{\mu\nu} \eta_{\lambda} \eta_{\nu\mu}^{\lambda} + (q - r)^{\mu\nu} \eta_{\lambda} \eta_{\nu\mu}^{\lambda} + (r - p)^{\mu\nu} \eta_{\lambda} \eta_{\nu\mu}^{\lambda}]$$

Vértice de gluón -4:

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \Gamma_{\mu\nu\lambda\sigma}^{abc\rho} \Gamma_{\nu\mu\lambda\sigma}^{abc\rho} \\ &= ijk g^{\mu\nu\rho\sigma} ijk g_{\nu\mu\rho\sigma} f^{abcde} f_{abcde} (\eta^{\mu\lambda} \eta_{\nu\sigma} - \eta^{\nu\lambda} \eta_{\mu\sigma}) \\ &\quad - ijk g^{\mu\nu\rho\sigma} ijk g_{\nu\mu\rho\sigma} f^{abcde} f_{abcde} (\eta^{\mu\sigma} \eta_{\nu\lambda} - \eta^{\nu\sigma} \eta_{\mu\lambda}) \\ &\quad - ijk g^{\mu\nu\rho\sigma} ijk g_{\nu\mu\rho\sigma} f^{abcde} f_{abcde} (\eta^{\mu\nu\lambda\sigma} \eta_{\mu\nu\sigma\lambda} - \eta^{\nu\mu\lambda\sigma} \eta_{\nu\mu\sigma\lambda}) \end{aligned}$$

Propagador Ghost:

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle C^{ab} C_{ba} \delta^{\mu\nu} \delta_{\nu\mu}(p, q) = ijk \delta^{ba} \delta_{ab} \delta^{\nu\mu} \delta_{\mu\nu} \rho\sigma\lambda\Omega / \omega \eta \xi \epsilon \phi \psi$$

Vértice c ζ g:

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \Gamma^{ab} \Gamma_{ba} \Gamma^{\mu\nu} \Gamma_{\nu\mu} \delta^{\mu\nu} \delta_{\nu\mu}(p, q, r) = gf^{abc} gf_{abc} ijk \delta^{ba} \delta_{ab} \delta^{\nu\mu} \delta_{\mu\nu} \rho^{\mu\nu} \rho_{\nu\mu} \sigma\lambda\Omega / \omega \eta \xi \epsilon \phi \psi$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle Z[ijk, \epsilon, \xi]$$

$$= \exp(ijk g \int_v^\mu d_\rho^\sigma \lambda xyz \dots n \delta / ijk \xi^{abcd} \xi_{abcd}(xyz \dots n) f \lambda_{\mu\nu\rho\sigma}^{abcd} f \mathcal{L}_{\mu\nu\rho\sigma}^{abcd} f \lambda_{abcd}^{\mu\nu\rho\sigma} f \mathcal{L}_{abcd}^{\mu\nu\rho\sigma} \partial \theta^{\mu\nu} \partial \theta_{\mu\nu} ijk \delta$$

$$/ \delta ijk_{\mu\nu}^{abc}(xyz \dots n) ijk \delta$$

$$\frac{ijk g \int_v^\mu d_\rho^\sigma \lambda xyz \dots n \frac{\delta \epsilon^{abc} \epsilon_{abc}(xyz \dots n)}{ijk \xi^{abcd} \xi_{abcd}(xyz \dots n) \partial \theta^{\mu\nu} \partial \theta_{\mu\nu} f \lambda_{\mu\nu\rho\sigma}^{abcd} f \mathcal{L}_{\mu\nu\rho\sigma}^{abcd} f \lambda_{abcd}^{\mu\nu\rho\sigma} f \mathcal{L}_{abcd}^{\mu\nu\rho\sigma}}{\delta ijk_{\mu\nu}^{abc}(xyz \dots n) ijk \delta}}{/ \delta \epsilon_{\mu\nu}^{abc}(xyz \dots n) x \exp(- \frac{\delta ijk_{\mu\nu}^{abc}(xyz \dots n) \delta ijk_{\nu\mu}^{abc}(xyz \dots n)}{\delta ijk_{\mu\nu}^{abc}(xyz \dots n) \delta ijk_{\nu\mu}^{abc}(xyz \dots n)}}}$$

$$* Z_0[ijk, \epsilon, \xi]$$

$$= \exp(- \int_v^\mu d_{abcd}^{\mu\nu\rho\sigma} d_{\mu\nu\rho\sigma}^{abcd} \Delta \lambda \nabla \Omega (xyz \dots n) C^{abcd} C_{\mu\nu\rho\sigma} C^{\mu\nu\rho\sigma} C_{abcd} \theta \lambda \Omega (x$$

$$- y) \epsilon_{\mu\nu\rho\sigma}^{abcd} \epsilon_{abcd}^{\mu\nu\rho\sigma} (xyz \dots n) \exp(- \frac{1}{2 \int_v^\mu d_{abcd}^{\mu\nu\rho\sigma} d_{\mu\nu\rho\sigma}^{abcd} \Delta \lambda \nabla \Omega} (xyz \dots n) \partial \Delta ijk_{\mu\nu\rho\sigma}^{abcd} \partial \nabla_{abcd}^{\mu\nu\rho\sigma} C^{abcd} C_{\mu\nu\rho\sigma} C^{\mu\nu\rho\sigma} C_{abcd} \theta \lambda \Omega (x$$

$$- y) \epsilon_{\mu\nu\rho\sigma}^{abcd} \epsilon_{abcd}^{\mu\nu\rho\sigma} (xyz \dots n)$$



b. Estructuras constantes antisimétricas.

$$\begin{aligned} \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^a, T^b = if^{abc}T^c + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^b, T^a = if^{abc}T^c + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^c, T^a = if^{abc}T^b + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^c, T^b = if^{abc}T^a + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^a, T^c = if^{abc}T^b + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^b, T^c = if^{abc}T^a + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^a, T^b = if^{bac}T^c + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^c, T^a = if^{bac}T^b + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^c, T^b = if^{bac}T^a + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^a, T^c = if^{bac}T^b + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^b, T^c = if^{bac}T^a + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^a, T^b = if^{cba}T^c + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^b, T^a = if^{cba}T^c + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^c, T^a = if^{cba}T^b + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^c, T^b = if^{cba}T^a + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^a, T^c = if^{cba}T^b + \hat{H} | \psi \rangle = E_\psi | \psi \rangle [T^b, T^c = if^{cba}T^a] = \xi_{\lambda\Omega\psi}^{\sigma\zeta} \Sigma \int \int \int \int \hbar \phi \text{I} \aleph \mathfrak{Z} \aleph \text{D} \aleph \text{I} \aleph \aleph \text{D} \zeta \pi m c^{\mathbb{R}^4} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle = E_\psi | \psi \rangle \text{tr} T^a T^b = \frac{1}{2} \delta^{ab} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \text{tr} T^b T^a = \frac{1}{2} \delta^{ba} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \text{tr} T^a T^b = \frac{1}{2} \delta^{ba} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \text{tr} T^b T^a = \frac{1}{2} \delta^{ab} = \xi_{\lambda\Omega\psi}^{\sigma\zeta} \Sigma \int \int \int \int \hbar \phi \text{I} \aleph \mathfrak{Z} \aleph \text{D} \aleph \text{I} \aleph \aleph \text{D} \zeta \pi m c^{\mathbb{R}^4} \end{aligned}$$

c. Campo de Gauge.

$$\begin{aligned} \hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu = A_\mu^a T^a + \hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu = A_\mu^b T^b + \hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu = A_\mu^c T^c + \hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu = A_\mu^{abc} T^{abc} = \xi_{\lambda\Omega\psi}^{\sigma\zeta} \Sigma \int \int \int \int \hbar \phi \text{I} \aleph \mathfrak{Z} \aleph \text{D} \aleph \text{I} \aleph \aleph \text{D} \zeta \pi m c^{\mathbb{R}^4} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\mu\nu} = \partial_\mu A_\nu - \partial_\nu A_\mu - i[A_\mu, A_\nu] + \hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\nu\mu} = \partial_\nu A_\mu - \partial_\mu A_\nu - i[A_\nu, A_\mu] = \xi_{\lambda\Omega\psi}^{\sigma\zeta} \Sigma \int \int \int \int \hbar \phi \text{I} \aleph \mathfrak{Z} \aleph \text{D} \aleph \text{I} \aleph \aleph \text{D} \zeta \pi m c^{\mathbb{R}^4} \end{aligned}$$

d. Covariante Derivada.

$$\begin{aligned} \hat{H} | \psi \rangle = E_\psi | \psi \rangle D_\mu \psi = \partial_\mu \psi - i A_\mu \psi + \hat{H} | \psi \rangle = E_\psi | \psi \rangle D_\nu \psi = \partial_\nu \psi - i A_\nu \psi + \hat{H} | \psi \rangle = E_\psi | \psi \rangle D_{\mu\nu} \psi = \partial_{\mu\nu} \psi - i A_{\mu\nu} \psi + \hat{H} | \psi \rangle = E_\psi | \psi \rangle D_{\nu\mu} \psi = \partial_{\nu\mu} \psi - i A_{\nu\mu} \psi = \xi_{\lambda\Omega\psi}^{\sigma\zeta} \Sigma \int \int \int \int \hbar \phi \text{I} \aleph \mathfrak{Z} \aleph \text{D} \aleph \text{I} \aleph \aleph \text{D} \zeta \pi m c^{\mathbb{R}^4} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle = E_\psi | \psi \rangle D_\mu \psi^i &= \partial_\nu \psi^i - i A_\mu^a T^a (R)_j^i \psi^j, j + \hat{H} | \psi \rangle = E_\psi | \psi \rangle D_\nu \psi^i \\ &= \partial_\mu \psi^i - i A_\nu^a T^a (R)_j^i \psi^j, j + \hat{H} | \psi \rangle = E_\psi | \psi \rangle D_{\mu\nu} \psi^{ij} \\ &= \partial_{\nu\mu} \psi^{ij} - ij A_{\mu\nu}^{abc} T^{abc} (R)_i^j \psi^j, i + \hat{H} | \psi \rangle = E_\psi | \psi \rangle D_{\nu\mu} \psi^{ji} \\ &= \partial_{\mu\nu} \psi^{ji} - ji A_{\nu\mu}^{abc} T^{abc} (R)_j^i \psi^i, j + \hat{H} | \psi \rangle = E_\psi | \psi \rangle D_{\mu\nu\nu\mu} \psi^{ijji} \\ &= \partial_{\nu\mu\nu\mu} \psi^{jiii} - jiii A_{\mu\nu}^{abc} T^{abc} (R)_{jii}^{jii} \psi^{jii} ijji, jiii \\ &= \xi_{\lambda\Omega\psi}^{\sigma\zeta} \Sigma \int \int \int \int \hbar \phi \text{I} \aleph \mathfrak{Z} \aleph \text{D} \aleph \text{I} \aleph \aleph \text{D} \zeta \pi m c^{\mathbb{R}^4} \end{aligned}$$

$$\begin{aligned} \hat{H}|\psi\rangle &= E_\psi|\psi\rangle D_\mu\phi = \partial_\mu\phi - i[A_\mu, \phi] + \hat{H}|\psi\rangle = E_\psi|\psi\rangle D_\nu\phi = \partial_\nu\phi - i[A_\nu, \phi] + \hat{H}|\psi\rangle = E_\psi|\psi\rangle D_{\mu\nu}\phi \\ &= \partial_{\mu\nu}\phi - ij[A_{\mu\nu}, \phi] + \hat{H}|\psi\rangle = E_\psi|\psi\rangle D_{\nu\mu}\phi = \partial_{\nu\mu}\phi - ji[A_{\nu\mu}, \phi] + \hat{H}|\psi\rangle \\ &= E_\psi|\psi\rangle D_{\mu\nu\nu\mu}\phi = \partial_{\mu\nu\nu\mu}\phi - ijji[A_{\mu\nu\nu\mu}, \phi] = \xi_{\lambda\Omega\psi}^{\sigma\zeta} \sum \int \int \int \int \hbar \mathfrak{C} \mathfrak{H} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \mathfrak{H} \mathfrak{K} \mathfrak{Z} \mathfrak{C} \pi m c^{\mathbb{R}^4} \end{aligned}$$

e. Dinámicas de Yang – Mills.

$$\begin{aligned} \hat{H}|\psi\rangle &= E_\psi|\psi\rangle S_{YM} = \frac{1}{2g^2} \int d^4x \operatorname{tr} F^{\mu\nu} F_{\mu\nu} + \hat{H}|\psi\rangle = E_\psi|\psi\rangle S_{YM} = \frac{1}{2g^2} \int d^4x \operatorname{tr} F^{\nu\mu} F_{\nu\mu} + \hat{H}|\psi\rangle \\ \psi\rangle &= E_\psi|\psi\rangle S_{YM} = \frac{n^\infty}{ng^\infty} \int \int \int \int_{v\mu}^{\mu\nu} \mu\nu\nu\mu d^\infty x \operatorname{tr} F^{\mu\nu\nu\mu} F_{\mu\nu\nu\mu} = \xi_{\lambda\Omega\psi}^{\sigma\zeta} \sum \int \int \int \int \hbar \mathfrak{C} \mathfrak{H} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \mathfrak{H} \mathfrak{K} \mathfrak{Z} \mathfrak{C} \pi m c^{\mathbb{R}^4} \end{aligned}$$

$$\begin{aligned} \hat{H}|\psi\rangle &= E_\psi|\psi\rangle * F^{\mu\nu} = \frac{1}{2} \epsilon^{\mu\nu\rho\sigma} F_{\rho\sigma} + \hat{H}|\psi\rangle = E_\psi|\psi\rangle * F^{\nu\mu} = \frac{1}{2} \epsilon^{\nu\mu\rho\sigma} F_{\rho\sigma} + \hat{H}|\psi\rangle = E_\psi|\psi\rangle * \\ F^{\mu\nu} &= \frac{1}{2} \epsilon^{\mu\nu\sigma\rho} F_{\sigma\rho} + \hat{H}|\psi\rangle = E_\psi|\psi\rangle * F^{\nu\mu} = \frac{1}{2} \epsilon^{\nu\mu\sigma\rho} F_{\sigma\rho} = \xi_{\lambda\Omega\psi}^{\sigma\zeta} \sum \int \int \int \int \hbar \mathfrak{C} \mathfrak{H} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \mathfrak{H} \mathfrak{K} \mathfrak{Z} \mathfrak{C} \pi m c^{\mathbb{R}^4} \end{aligned}$$

f. Rescaling.

$$\begin{aligned} \hat{H}|\psi\rangle &= E_\psi|\psi\rangle \tilde{A}_\mu = \frac{1}{g} A_\mu + \hat{H}|\psi\rangle = E_\psi|\psi\rangle \tilde{A}_\nu = \frac{1}{g} A_\nu + \hat{H}|\psi\rangle = E_\psi|\psi\rangle \tilde{A}_{\mu\nu} = \frac{1}{g} A_{\mu\nu} + \hat{H}|\psi\rangle \\ &= E_\psi|\psi\rangle \tilde{A}_{\nu\mu} = \frac{1}{g} A_{\nu\mu} + \mathbf{F}_{\mu\nu} = \partial_u \tilde{A}_\nu - \partial_\nu \tilde{A}_u - ig[\tilde{A}_u, \tilde{A}_\nu] + \mathbf{F}_{\nu\mu} \\ &= \partial_\nu \tilde{A}_\mu - \partial_\mu \tilde{A}_\nu - ig[\tilde{A}_\nu, \tilde{A}_\mu] = \xi_{\lambda\Omega\psi}^{\sigma\zeta} \sum \int \int \int \int \hbar \mathfrak{C} \mathfrak{H} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \mathfrak{H} \mathfrak{K} \mathfrak{Z} \mathfrak{C} \pi m c^{\mathbb{R}^4} \\ \hat{H}|\psi\rangle &= E_\psi|\psi\rangle S_{YM} = \frac{1}{2g^2} \int d^4x \operatorname{tr} F^{\mu\nu} F_{\mu\nu} = -\frac{1}{2} \int d^4x \operatorname{tr} F^{\mu\nu} F_{\mu\nu} \\ \hat{H}|\psi\rangle &= E_\psi|\psi\rangle S_{YM} = \frac{1}{2g^2} \int d^4x \operatorname{tr} F^{\nu\mu} F_{\nu\mu} = -\frac{1}{2} \int d^4x \operatorname{tr} F^{\nu\mu} F_{\nu\mu} \\ \hat{H}|\psi\rangle &= E_\psi|\psi\rangle S_{YM} = \frac{n}{ng^\infty} \int d^\infty x \operatorname{tr} F^{\nu\mu} F_{\nu\mu} = -\frac{n}{n-1} \int d^\infty x \operatorname{tr} F^{\nu\mu} F_{\nu\mu} \\ \hat{H}|\psi\rangle &= E_\psi|\psi\rangle S_{YM} = \frac{n}{ng^\infty} \int d^\infty x \operatorname{tr} F^{\mu\nu} F_{\mu\nu} = -\frac{n}{n-1} \int d^\infty x \operatorname{tr} F^{\mu\nu} F_{\mu\nu} \end{aligned}$$

g. Simetría de Gauge.

$$\begin{aligned} \hat{H}|\psi\rangle &= E_\psi|\psi\rangle A_\mu \rightarrow \Omega(x) A_\mu \Omega^{-1}(x) + i\Omega(x) \partial_\mu \Omega^{-1}(x) \\ \hat{H}|\psi\rangle &= E_\psi|\psi\rangle A_\nu \rightarrow \Omega(x) A_\nu \Omega^{-1}(x) + i\Omega(x) \partial_\nu \Omega^{-1}(x) \\ \hat{H}|\psi\rangle &= E_\psi|\psi\rangle A_{\mu\nu} \rightarrow \Omega(x) A_{\mu\nu} \Omega^{-1}(x) + i\Omega(x) \partial_{\mu\nu} \Omega^{-1}(x) \\ \hat{H}|\psi\rangle &= E_\psi|\psi\rangle A_{\nu\mu} \rightarrow \Omega(x) A_{\nu\mu} \Omega^{-1}(x) + i\Omega(x) \partial_{\nu\mu} \Omega^{-1}(x) \end{aligned}$$



$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \Omega(y) A_\mu \Omega^{-1}(y) i\Omega(y) \partial_\mu \Omega^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_v \rightarrow \Omega(y) A_v \Omega^{-1}(y) i\Omega(y) \partial_v \Omega^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \Omega(y) A_{\mu\nu} \Omega^{-1}(y) i\Omega(y) \partial_{\mu\nu} \Omega^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{v\mu} \rightarrow \Omega(y) A_{v\mu} \Omega^{-1}(y) i\Omega(y) \partial_{v\mu} \Omega^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \Omega(z) A_\mu \Omega^{-1}(z) i\Omega(z) \partial_\mu \Omega^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_v \rightarrow \Omega(z) A_v \Omega^{-1}(z) i\Omega(z) \partial_v \Omega^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \Omega(z) A_{\mu\nu} \Omega^{-1}(z) i\Omega(z) \partial_{\mu\nu} \Omega^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{v\mu} \rightarrow \Omega(z) A_{v\mu} \Omega^{-1}(z) i\Omega(z) \partial_{v\mu} \Omega^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \Omega(\infty) A_\mu \Omega^{-1}(\infty) i\Omega(\infty) \partial_\mu \Omega^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_v \rightarrow \Omega(\infty) A_v \Omega^{-1}(\infty) i\Omega(\infty) \partial_v \Omega^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \Omega(\infty) A_{\mu\nu} \Omega^{-1}(\infty) i\Omega(\infty) \partial_{\mu\nu} \Omega^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{v\mu} \rightarrow \Omega(\infty) A_{v\mu} \Omega^{-1}(\infty) i\Omega(\infty) \partial_{v\mu} \Omega^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \Omega(x) A_\mu \Omega^{-1}(x) j\Omega(x) \partial_\mu \Omega^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_v \rightarrow \Omega(x) A_v \Omega^{-1}(x) j\Omega(x) \partial_v \Omega^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \Omega(x) A_{\mu\nu} \Omega^{-1}(x) j\Omega(x) \partial_{\mu\nu} \Omega^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{v\mu} \rightarrow \Omega(x) A_{v\mu} \Omega^{-1}(x) j\Omega(x) \partial_{v\mu} \Omega^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \Omega(y) A_\mu \Omega^{-1}(y) j\Omega(y) \partial_\mu \Omega^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_v \rightarrow \Omega(y) A_v \Omega^{-1}(y) j\Omega(y) \partial_v \Omega^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \Omega(y) A_{\mu\nu} \Omega^{-1}(y) j\Omega(y) \partial_{\mu\nu} \Omega^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{v\mu} \rightarrow \Omega(y) A_{v\mu} \Omega^{-1}(y) j\Omega(y) \partial_{v\mu} \Omega^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \Omega(z) A_\mu \Omega^{-1}(z) j\Omega(z) \partial_\mu \Omega^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_v \rightarrow \Omega(z) A_v \Omega^{-1}(z) j\Omega(z) \partial_v \Omega^{-1}(z)$$



$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \Omega(z) A_{\mu\nu} \Omega^{-1}(z) j\Omega(z) \partial_{\mu\nu} \Omega^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\nu\mu} \rightarrow \Omega(z) A_{\nu\mu} \Omega^{-1}(z) j\Omega(z) \partial_{\nu\mu} \Omega^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \Omega(\infty) A_\mu \Omega^{-1}(\infty) j\Omega(\infty) \partial_\mu \Omega^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\nu \rightarrow \Omega(\infty) A_\nu \Omega^{-1}(\infty) j\Omega(\infty) \partial_\nu \Omega^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \Omega(\infty) A_{\mu\nu} \Omega^{-1}(\infty) j\Omega(\infty) \partial_{\mu\nu} \Omega^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\nu\mu} \rightarrow \Omega(\infty) A_{\nu\mu} \Omega^{-1}(\infty) j\Omega(\infty) \partial_{\nu\mu} \Omega^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\mu\nu} \rightarrow \Omega(x) F_{\mu\nu} \Omega^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\nu\mu} \rightarrow \Omega(x) F_{\nu\mu} \Omega^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\mu\nu} \rightarrow \Omega(y) F_{\mu\nu} \Omega^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\nu\mu} \rightarrow \Omega(y) F_{\nu\mu} \Omega^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\mu\nu} \rightarrow \Omega(z) F_{\mu\nu} \Omega^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\nu\mu} \rightarrow \Omega(z) F_{\nu\mu} \Omega^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\mu\nu} \rightarrow \Omega(\infty) F_{\mu\nu} \Omega^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\nu\mu} \rightarrow \Omega(\infty) F_{\nu\mu} \Omega^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \mathcal{U}(x) A_\mu \mathcal{U}^{-1}(x) i\mathcal{U}(x) \partial_\mu \mathcal{U}^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\nu \rightarrow \mathcal{U}(x) A_\nu \mathcal{U}^{-1}(x) i\mathcal{U}(x) \partial_\nu \mathcal{U}^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \mathcal{U}(x) A_{\mu\nu} \mathcal{U}^{-1}(x) i\mathcal{U}(x) \partial_{\mu\nu} \mathcal{U}^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\nu\mu} \rightarrow \mathcal{U}(x) A_{\nu\mu} \mathcal{U}^{-1}(x) i\mathcal{U}(x) \partial_{\nu\mu} \mathcal{U}^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \mathcal{U}(y) A_\mu \mathcal{U}^{-1}(y) i\mathcal{U}(y) \partial_\mu \mathcal{U}^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\nu \rightarrow \mathcal{U}(y) A_\nu \mathcal{U}^{-1}(y) i\mathcal{U}(y) \partial_\nu \mathcal{U}^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \mathcal{U}(y) A_{\mu\nu} \mathcal{U}^{-1}(y) i\mathcal{U}(y) \partial_{\mu\nu} \mathcal{U}^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\nu\mu} \rightarrow \mathcal{U}(y) A_{\nu\mu} \mathcal{U}^{-1}(y) i\mathcal{U}(y) \partial_{\nu\mu} \mathcal{U}^{-1}(y)$$



$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \mathcal{U}(z) A_\mu \mathcal{U}^{-1}(z) i\mathcal{U}(z) \partial_\mu \mathcal{U}^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\nu \rightarrow \mathcal{U}(z) A_\nu \mathcal{U}^{-1}(z) i\mathcal{U}(z) \partial_\nu \mathcal{U}^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \mathcal{U}(z) A_{\mu\nu} \mathcal{U}^{-1}(z) i\mathcal{U}(z) \partial_{\mu\nu} \mathcal{U}^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\nu\mu} \rightarrow \mathcal{U}(z) A_{\nu\mu} \mathcal{U}^{-1}(z) i\mathcal{U}(z) \partial_{\nu\mu} \mathcal{U}^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \mathcal{U}(\infty) A_\mu \mathcal{U}^{-1}(\infty) i\mathcal{U}(\infty) \partial_\mu \mathcal{U}^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\nu \rightarrow \Omega(\infty) A_\nu \mathcal{U}^{-1}(\infty) i\mathcal{U}(\infty) \partial_\nu \mathcal{U}^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \Omega(\infty) A_{\mu\nu} \mathcal{U}^{-1}(\infty) i\mathcal{U}(\infty) \partial_{\mu\nu} \mathcal{U}^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\nu\mu} \rightarrow \Omega(\infty) A_{\nu\mu} \mathcal{U}^{-1}(\infty) i\mathcal{U}(\infty) \partial_{\nu\mu} \mathcal{U}^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \mathcal{U}(x) A_\mu \mathcal{U}^{-1}(x) j\mathcal{U}(x) \partial_\mu \mathcal{U}^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\nu \rightarrow \mathcal{U}(x) A_\nu \mathcal{U}^{-1}(x) j\mathcal{U}(x) \partial_\nu \mathcal{U}^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \mathcal{U}(x) A_{\mu\nu} \mathcal{U}^{-1}(x) j\mathcal{U}(x) \partial_{\mu\nu} \mathcal{U}^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\nu\mu} \rightarrow \mathcal{U}(x) A_{\nu\mu} \mathcal{U}^{-1}(x) j\mathcal{U}(x) \partial_{\nu\mu} \mathcal{U}^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \mathcal{U}(y) A_\mu \mathcal{U}^{-1}(y) j\mathcal{U}(y) \partial_\mu \mathcal{U}^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\nu \rightarrow \mathcal{U}(y) A_\nu \mathcal{U}^{-1}(y) j\mathcal{U}(y) \partial_\nu \mathcal{U}^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \mathcal{U}(y) A_{\mu\nu} \mathcal{U}^{-1}(y) j\mathcal{U}(y) \partial_{\mu\nu} \mathcal{U}^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\nu\mu} \rightarrow \mathcal{U}(y) A_{\nu\mu} \mathcal{U}^{-1}(y) j\mathcal{U}(y) \partial_{\nu\mu} \mathcal{U}^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \mathcal{U}(z) A_\mu \mathcal{U}^{-1}(z) j\mathcal{U}(z) \partial_\mu \mathcal{U}^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\nu \rightarrow \mathcal{U}(z) A_\nu \mathcal{U}^{-1}(z) j\mathcal{U}(z) \partial_\nu \mathcal{U}^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \mathcal{U}(z) A_{\mu\nu} \mathcal{U}^{-1}(z) j\mathcal{U}(z) \partial_{\mu\nu} \mathcal{U}^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\nu\mu} \rightarrow \mathcal{U}(z) A_{\nu\mu} \mathcal{U}^{-1}(z) j\mathcal{U}(z) \partial_{\nu\mu} \mathcal{U}^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\mu \rightarrow \mathcal{U}(\infty) A_\mu \mathcal{U}^{-1}(\infty) j\mathcal{U}(\infty) \partial_\mu \mathcal{U}^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_\nu \rightarrow \mathcal{U}(\infty) A_\nu \mathcal{U}^{-1}(\infty) j\mathcal{U}(\infty) \partial_\nu \mathcal{U}^{-1}(\infty)$$



$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\mu\nu} \rightarrow \mathcal{U}(\infty) A_{\mu\nu} \mathcal{U}^{-1}(\infty) j \mathcal{U}(\infty) \partial_{\mu\nu} \mathcal{U}^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle A_{\nu\mu} \rightarrow \mathcal{U}(\infty) A_{\nu\mu} \mathcal{U}^{-1}(\infty) j \mathcal{U}(\infty) \partial_{\nu\mu} \mathcal{U}^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\mu\nu} \rightarrow \mathcal{U}(x) F_{\mu\nu} \mathcal{U}^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\nu\mu} \rightarrow \mathcal{U}(x) F_{\nu\mu} \mathcal{U}^{-1}(x)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\mu\nu} \rightarrow \mathcal{U}(y) F_{\mu\nu} \mathcal{U}^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\nu\mu} \rightarrow \mathcal{U}(y) F_{\nu\mu} \mathcal{U}^{-1}(y)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\mu\nu} \rightarrow \mathcal{U}(z) F_{\mu\nu} \mathcal{U}^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\nu\mu} \rightarrow \mathcal{U}(z) F_{\nu\mu} \mathcal{U}^{-1}(z)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\mu\nu} \rightarrow \mathcal{U}(\infty) F_{\mu\nu} \mathcal{U}^{-1}(\infty)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle F_{\nu\mu} \rightarrow \mathcal{U}(\infty) F_{\nu\mu} \mathcal{U}^{-1}(\infty)$$

h. Ecuaciones de Transportación Paralela.

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle i \frac{d\omega}{d\tau} = \frac{dx^\mu}{d\tau} A_\mu(x) \omega + \hat{H} | \psi \rangle = E_\psi | \psi \rangle j \frac{d\omega}{d\tau} = \frac{dx^\mu}{d\tau} A_\mu(x) \omega$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle i \frac{d\omega}{d\tau} = \frac{dy^\mu}{d\tau} A_\mu(y) \omega + \hat{H} | \psi \rangle = E_\psi | \psi \rangle j \frac{d\omega}{d\tau} = \frac{dy^\mu}{d\tau} A_\mu(y) \omega$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle i \frac{d\omega}{d\tau} = \frac{dz^\mu}{d\tau} A_\mu(z) \omega + \hat{H} | \psi \rangle = E_\psi | \psi \rangle j \frac{d\omega}{d\tau} = \frac{dz^\mu}{d\tau} A_\mu(z) \omega$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle i \frac{d\omega}{d\tau} = \frac{d\infty^\mu}{d\tau} A_\mu(\infty) \omega + \hat{H} | \psi \rangle = E_\psi | \psi \rangle j \frac{d\omega}{d\tau} = \frac{d\infty^\mu}{d\tau} A_\mu(\infty) \omega$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle i \frac{d\omega}{d\tau} = \frac{dx^v}{d\tau} A_v(x) \omega + \hat{H} | \psi \rangle = E_\psi | \psi \rangle j \frac{d\omega}{d\tau} = \frac{dx^v}{d\tau} A_v(x) \omega$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle i \frac{d\omega}{d\tau} = \frac{dy^v}{d\tau} A_v(y) \omega + \hat{H} | \psi \rangle = E_\psi | \psi \rangle j \frac{d\omega}{d\tau} = \frac{dy^v}{d\tau} A_v(y) \omega$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle i \frac{d\omega}{d\tau} = \frac{dz^v}{d\tau} A_v(z) \omega + \hat{H} | \psi \rangle = E_\psi | \psi \rangle j \frac{d\omega}{d\tau} = \frac{dz^v}{d\tau} A_v(z) \omega$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle i \frac{d\omega}{d\tau} = \frac{d\infty^v}{d\tau} A_v(\infty) \omega + \hat{H} | \psi \rangle = E_\psi | \psi \rangle j \frac{d\omega}{d\tau} = \frac{d\infty^v}{d\tau} A_v(\infty) \omega$$



$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle j, i \frac{d\omega}{d\tau} = \frac{dx^{\mu\nu}}{d\tau} A_{\mu\nu}(x)\omega + \hat{H}|\psi\rangle = E_\psi|\psi\rangle i, j \frac{d\omega}{d\tau} = \frac{dx^{\mu\nu}}{d\tau} A_{\mu\nu}(x)\omega$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle j, i \frac{d\omega}{d\tau} = \frac{dy^{\mu\nu}}{d\tau} A_{\mu\nu}(y)\omega + \hat{H}|\psi\rangle = E_\psi|\psi\rangle i, j \frac{d\omega}{d\tau} = \frac{dy^{\mu\nu}}{d\tau} A_{\mu\nu}(y)\omega$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle j, i \frac{d\omega}{d\tau} = \frac{dz^{\mu\nu}}{d\tau} A_{\mu\nu}(z)\omega + \hat{H}|\psi\rangle = E_\psi|\psi\rangle i, j \frac{d\omega}{d\tau} = \frac{dz^{\mu\nu}}{d\tau} A_{\mu\nu}(z)\omega$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle j, i \frac{d\omega}{d\tau} = \frac{d\infty^{\mu\nu}}{d\tau} A_{\mu\nu}(\infty)\omega + \hat{H}|\psi\rangle = E_\psi|\psi\rangle i, j \frac{d\omega}{d\tau} = \frac{d\infty^{\mu\nu}}{d\tau} A_{\mu\nu}(\infty)\omega$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle j, i \frac{d\omega}{d\tau} = \frac{dx^{\nu\mu}}{d\tau} A_{\nu\mu}(x)\omega + \hat{H}|\psi\rangle = E_\psi|\psi\rangle i, j \frac{d\omega}{d\tau} = \frac{dx^{\nu\mu}}{d\tau} A_{\nu\mu}(x)\omega$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle j, i \frac{d\omega}{d\tau} = \frac{dy^{\nu\mu}}{d\tau} A_{\nu\mu}(y)\omega + \hat{H}|\psi\rangle = E_\psi|\psi\rangle i, j \frac{d\omega}{d\tau} = \frac{dy^{\nu\mu}}{d\tau} A_{\nu\mu}(y)\omega$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle j, i \frac{d\omega}{d\tau} = \frac{dz^{\nu\mu}}{d\tau} A_{\nu\mu}(z)\omega + \hat{H}|\psi\rangle = E_\psi|\psi\rangle i, j \frac{d\omega}{d\tau} = \frac{dz^{\nu\mu}}{d\tau} A_{\nu\mu}(z)\omega$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle j, i \frac{d\omega}{d\tau} = \frac{d\infty^{\nu\mu}}{d\tau} A_{\nu\mu}(\infty)\omega + \hat{H}|\psi\rangle = E_\psi|\psi\rangle i, j \frac{d\omega}{d\tau} = \frac{d\infty^{\nu\mu}}{d\tau} A_{\nu\mu}(\infty)\omega$$

h. Movimiento de partículas.

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle U[xyz_i, xyz_f; C] = P \exp(i \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^\mu}{d\tau} A_\mu(xyz(\tau))) = P \exp(i \int_{xyzi}^{xyzf} A)$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle U[xyz_f, xyz_i; C] = P \exp(i \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^\mu}{d\tau} A_\mu(xyz(\tau))) = P \exp(i \int_{xyzf}^{xyzi} A)$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle U[xyz_i, xyz_f; C] = P \exp(j \int_{\tau_i}^{\tau_f} d\tau \frac{dx^\mu}{d\tau} A_\mu(xyz(\tau))) = P \exp(j \int_{xyzi}^{xyzf} A)$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle U[xyz_f, xyz_i; C] = P \exp(j \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^\mu}{d\tau} A_\mu(xyz(\tau))) = P \exp(j \int_{xyzf}^{xyzi} A)$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle U[xyz_i, xyz_f; C] = P \exp(i \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^v}{d\tau} A_v(xyz(\tau))) = P \exp(i \int_{xyzi}^{xyzf} A)$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle U[xyz_f, xyz_i; C] = P \exp(i \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^v}{d\tau} A_v(xyz(\tau))) = P \exp(i \int_{xyzf}^{xyzi} A)$$



$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_i, xyz_f; C] = Pexp(j \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^v}{d\tau} A_v(xyz(\tau))) = Pexp(j \int_{xyzi}^{xyzf} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_f, xyz_i; C] = Pexp(j \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^v}{d\tau} A_v(xyz(\tau))) = Pexp(j \int_{xyzf}^{xyzi} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_i, xyz_f; C] = Pexp(i \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^{\mu\nu}}{d\tau} A_{\mu\nu}(xyz(\tau))) = Pexp(i \int_{xyzi}^{xyzf} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_f, xyz_i; C] = Pexp(i \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^{\mu\nu}}{d\tau} A_{\mu\nu}(xyz(\tau))) = Pexp(i \int_{xyzf}^{xyzi} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_i, xyz_f; C] = Pexp(j \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^{\mu\nu}}{d\tau} A_{\mu\nu}(xyz(\tau))) = Pexp(j \int_{xyzi}^{xyzf} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_f, xyz_i; C] = Pexp(j \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^{\mu\nu}}{d\tau} A_{\mu\nu}(xyz(\tau))) = Pexp(j \int_{xyzf}^{xyzi} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_i, xyz_f; C] = Pexp(i \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^{v\mu}}{d\tau} A_{v\mu}(xyz(\tau))) = Pexp(i \int_{xyzi}^{xyzf} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_f, xyz_i; C] = Pexp(i \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^{v\mu}}{d\tau} A_{v\mu}(xyz(\tau))) = Pexp(i \int_{xyzf}^{xyzi} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_i, xyz_f; C] = Pexp(j \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^{v\mu}}{d\tau} A_{v\mu}(xyz(\tau))) = Pexp(j \int_{xyzi}^{xyzf} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_f, xyz_i; C] = Pexp(j \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^{v\mu}}{d\tau} A_{v\mu}(xyz(\tau))) = Pexp(j \int_{xyzf}^{xyzi} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_i, xyz_f; C] = Pexp(i \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^\mu}{d\tau} A_\mu(xyz(\tau))) = Pexp(j \int_{xyzi}^{xyzf} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_f, xyz_i; C] = Pexp(i \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^\mu}{d\tau} A_\mu(xyz(\tau))) = Pexp(j \int_{xyzf}^{xyzi} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_i, xyz_f; C] = Pexp(j \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^\mu}{d\tau} A_\mu(xyz(\tau))) = Pexp(i \int_{xyzi}^{xyzf} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_f, xyz_i; C] = Pexp(j \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^\mu}{d\tau} A_\mu(xyz(\tau))) = Pexp(i \int_{xyzf}^{xyzi} A)$$



$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_i, xyz_f; C] = Pexp(i \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^v}{d\tau} A_v(xyz(\tau))) = Pexp(j \int_{xyzi}^{xyzf} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_f, xyz_i; C] = Pexp(i \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^v}{d\tau} A_v(xyz(\tau))) = Pexp(j \int_{xyzf}^{xyzi} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_i, xyz_f; C] = Pexp(j \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^v}{d\tau} A_v(xyz(\tau))) = Pexp(i \int_{xyzi}^{xyzf} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_f, xyz_i; C] = Pexp(j \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^v}{d\tau} A_v(xyz(\tau))) = Pexp(i \int_{xyzf}^{xyzi} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_i, xyz_f; C] = Pexp(i \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^{\mu\nu}}{d\tau} A_{\mu\nu}(xyz(\tau))) = Pexp(j \int_{xyzi}^{xyzf} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_f, xyz_i; C] = Pexp(i \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^{\mu\nu}}{d\tau} A_{\mu\nu}(xyz(\tau))) = Pexp(j \int_{xyzf}^{xyzi} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_i, xyz_f; C] = Pexp(j \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^{\mu\nu}}{d\tau} A_{\mu\nu}(xyz(\tau))) = Pexp(i \int_{xyzi}^{xyzf} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_f, xyz_i; C] = Pexp(j \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^{\mu\nu}}{d\tau} A_{\mu\nu}(xyz(\tau))) = Pexp(i \int_{xyzf}^{xyzi} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_i, xyz_f; C] = Pexp(i \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^{v\mu}}{d\tau} A_{v\mu}(xyz(\tau))) = Pexp(j \int_{xyzi}^{xyzf} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_f, xyz_i; C] = Pexp(i \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^{v\mu}}{d\tau} A_{v\mu}(xyz(\tau))) = Pexp(j \int_{xyzf}^{xyzi} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_i, xyz_f; C] = Pexp(j \int_{\tau_i}^{\tau_f} d\tau \frac{dxyz^{v\mu}}{d\tau} A_{v\mu}(xyz(\tau))) = Pexp(i \int_{xyzi}^{xyzf} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_f, xyz_i; C] = Pexp(j \int_{\tau_f}^{\tau_i} d\tau \frac{dxyz^{v\mu}}{d\tau} A_{v\mu}(xyz(\tau))) = Pexp(i \int_{xyzf}^{xyzi} A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_i, xyz_f; C] \rightarrow \Omega(xyz_i)U[xyz_i, xyz_f; C]\Omega^\dagger(x_f)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle U[xyz_f, xyz_i; C] \rightarrow \Omega(xyz_j)U[xyz_f, xyz_i; C]\Omega^\dagger(x_f)$$



$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle W[C] = \text{tr} P \exp(i \oint A) + \hat{H} | \psi \rangle = E_\psi | \psi \rangle W[C] = \text{tr} P \exp(f \oint A)$$

i. Cuantificación del grado de libertad.

$$\begin{aligned} \hat{H} | \psi \rangle = E_\psi | \psi \rangle S_w &= \int d\tau i w^\dagger \frac{dw}{dt} + \lambda(w^\dagger w - k) + w^\dagger A(xyz(\tau))w + [w_i, w_j^\dagger = \delta_{ij} + |i_1 \dots i_n\rangle \\ &= w_{i_1}^\dagger \dots w_{i_n}^\dagger | \xi_{\lambda\Omega\psi}^{\sigma\zeta} \Sigma \int \int \int \int \mathfrak{h} \Phi \mathfrak{B} \mathfrak{X} \mathfrak{Z} \mathfrak{J} \mathfrak{K} \mathfrak{L} \mathfrak{H} \mathfrak{I} \mathfrak{J} \mathfrak{K} \mathfrak{L} \mathfrak{M} \mathfrak{C}^{\mathbb{R}^4} \rangle \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle = E_\psi | \psi \rangle S_w &= \int d\tau j w^\dagger \frac{dw}{dt} + \lambda(w^\dagger w - k) + w^\dagger A(xyz(\tau))w + [w_j, w_i^\dagger = \delta_{ji} + |j_1 \dots j_n\rangle \\ &= w_{j_1}^\dagger \dots w_{j_n}^\dagger | \xi_{\lambda\Omega\psi}^{\sigma\zeta} \Sigma \int \int \int \int \mathfrak{h} \Phi \mathfrak{B} \mathfrak{X} \mathfrak{Z} \mathfrak{J} \mathfrak{K} \mathfrak{L} \mathfrak{H} \mathfrak{I} \mathfrak{J} \mathfrak{K} \mathfrak{L} \mathfrak{M} \mathfrak{C}^{\mathbb{R}^4} \rangle \end{aligned}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle Z_w[A] = \text{tr} P \exp(i \int d\tau A(\tau)) + \hat{H} | \psi \rangle = E_\psi | \psi \rangle Z_w[A] = \text{tr} P \exp(j \int d\tau A(\tau))$$

j. Término Theta.

$$\begin{aligned} \hat{H} | \psi \rangle = E_\psi | \psi \rangle S_\theta &= \frac{\theta}{16\pi^2} \int d^4 x \text{tr} * F^{\mu\nu} F_{\mu\nu} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle S_\theta \\ &= \frac{\theta}{16\pi^2} \int d^4 xyz \dots n \text{tr} * F^{\nu\mu} F_{\mu\nu} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle S_\theta \\ &= \frac{\theta}{16\pi^2} \int d^4 xyz \dots n \text{tr} * F^{\nu\mu} F_{\nu\mu} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle S_\theta \\ &= \frac{\theta}{16\pi^2} \int d^4 xyz \dots n \text{tr} * F^{\mu\nu} F_{\nu\mu} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle = E_\psi | \psi \rangle S_\theta &= \frac{\theta}{8\pi^2} \int d^4 x \partial_\mu K^\mu + \hat{H} | \psi \rangle = E_\psi | \psi \rangle S_\theta = \frac{\theta}{8\pi^2} \int d^4 xyz \dots n \partial_\nu K^\nu + \hat{H} | \psi \rangle \\ &= E_\psi | \psi \rangle S_\theta = \frac{\theta}{8\pi^2} \int d^4 xyz \dots n \partial_{\mu\nu} K^{\mu\nu} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle S_\theta \\ &= \frac{\theta}{8\pi^2} \int d^4 xyz \dots n \partial_{\nu\mu} K^{\nu\mu} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle = E_\psi | \psi \rangle K^\mu &= \epsilon^{\mu\nu\rho\sigma} \text{tr}(A_\nu \partial_\rho A_\sigma - \frac{2i}{3} A_\nu A_\rho A_\sigma) + \hat{H} | \psi \rangle = E_\psi | \psi \rangle K^\nu \\ &= \epsilon^{\nu\mu\sigma\rho} \text{tr}(A_\mu \partial_\sigma A_\rho A_\nu - \frac{2j}{3} A_\mu A_\sigma A_\rho A_\nu) \end{aligned}$$



k. Cuantificación Canónica de Yang – Mills.

$$\begin{aligned}
 \hat{H} | \psi \rangle = E_\psi | \psi \rangle L &= \frac{1}{2g^2} \text{tr} F^{\mu\nu} F_{\mu\nu} + \frac{\theta}{16\pi^2} \text{tr} * F^{\mu\nu} F_{\mu\nu} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle L \\
 &= \frac{1}{2g^2} \text{tr} F^{\nu\mu} F_{\nu\mu} + \frac{\theta}{16\pi^2} \text{tr} * F^{\nu\mu} F_{\nu\mu} + L \\
 &= \frac{1}{2g^2} \text{tr} \left(\lim_{n \rightarrow \infty} \left(1 + \frac{1}{n} \right)^n \prod_{\nu}^{\mu} \mu\nu\nu\mu \left(\sqrt{A^2 - B^2/B^2 - A^2} + \frac{\theta}{16\pi^2} \text{tr} \sqrt{A^2 \cdot \frac{B^2}{B^2} \cdot A^2} \right) \right) \\
 \hat{H} | \psi \rangle = E_\psi | \psi \rangle H &= g^{\mu\nu\rho\sigma} \text{tr} \left(\pi - \frac{\theta}{16\pi^{\mu\nu\rho\sigma}} B \right) e^{-\frac{i\omega t}{\mu\nu\rho\sigma}} + \frac{1}{g^{\mu\nu\rho\sigma}} \text{tr} B^{\mu\nu\rho\sigma} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle H \\
 &= g^{\nu\mu\sigma\rho} \text{tr} \left(\pi - \frac{\theta}{16\pi^{\nu\mu\sigma\rho}} B \right) e^{-i\omega t/\nu\mu\sigma\rho} + \frac{1}{g^{\nu\mu\sigma\rho}} \text{tr} B^{\nu\mu\sigma\rho}
 \end{aligned}$$

l. Construcción de un Espacio de Hilbert.

$$\begin{aligned}
 \hat{H} | \psi \rangle = E_\psi | \psi \rangle Q(w) &= \oint d^n x \text{tr} (\pi \cdot \delta A) = \frac{1}{g^n} \oint d^n x \text{tr} \left(E_i + \frac{\theta g^{\mu\nu\rho\sigma}}{16\pi^{\mu\nu\rho\sigma}} B_i \right) D_{iw} \\
 &= -\frac{1}{g^{\mu\nu\rho\sigma}} \oint d^n x \text{tr} (D_i E_i W_{\mu\nu\rho\sigma}) \\
 \hat{H} | \psi \rangle = E_\psi | \psi \rangle Q(w) &= \oint d^n xyz \dots n \text{tr} (\pi \cdot \delta A \cdot B) = \frac{1}{g^n} \oint d^n xyz \dots n \text{tr} \left(E_i + \frac{\theta g^{\mu\nu\rho\sigma}}{16\pi^{\mu\nu\rho\sigma}} B_i \right) D_{iw} \\
 &= -\frac{1}{g^{\mu\nu\rho\sigma}} \oint d^n x \text{tr} (D_i E_i W_{\mu\nu\rho\sigma}) \\
 \hat{H} | \psi \rangle = E_\psi | \psi \rangle Q(w) &= \oint d^n xyz \dots n \text{tr} (\pi \cdot \delta A \cdot B) = \frac{1}{g^n} \oint d^n xyz \dots n \text{tr} \left(E_j + \frac{\theta g^{\mu\nu\rho\sigma}}{16\pi^{\mu\nu\rho\sigma}} B_j \right) D_{jw} \\
 &= -\frac{1}{g^{\mu\nu\rho\sigma}} \oint d^n x \text{tr} (D_j E_j W_{\mu\nu\rho\sigma}) \\
 \hat{H} | \psi \rangle = E_\psi | \psi \rangle Q(w) &= \oint d^n xyz \dots n \text{tr} (\pi \cdot \delta A \cdot B) = \frac{1}{g^n} \oint d^n xyz \dots n \text{tr} \left(E_{i,j} + \frac{\theta g^{\mu\nu\rho\sigma}}{16\pi^{\mu\nu\rho\sigma}} B_{i,j} \right) D_{i,jw} \\
 &= -\frac{1}{g^{\mu\nu\rho\sigma}} \oint d^n x \text{tr} (D_{i,j} E_{i,j} W_{\mu\nu\rho\sigma}) \\
 \hat{H} | \psi \rangle = E_\psi | \psi \rangle Q(w) &= \oint d^n xyz \dots n \text{tr} (\pi \cdot \delta A \cdot B) = \frac{1}{g^n} \oint d^n xyz \dots n \text{tr} \left(E_{j,i} + \frac{\theta g^{\mu\nu\rho\sigma}}{16\pi^{\mu\nu\rho\sigma}} B_{j,i} \right) D_{j,iw} \\
 &= -\frac{1}{g^{\mu\nu\rho\sigma}} \oint d^n x \text{tr} (D_{j,i} E_{j,i} W_{\mu\nu\rho\sigma})
 \end{aligned}$$



$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle Q(w) = \oint d^n xyz \dots n \operatorname{tr}(\pi \cdot \delta A \cdot B) = \frac{1}{g^n} \oint d^n xyz \dots n \operatorname{tr} \left(E_i + \frac{\theta g^{\nu\mu\sigma\rho}}{16\pi^{\nu\mu\sigma\rho}} B_i \right) D_{i,w} \\ &= -\frac{1}{g^{\nu\mu\sigma\rho}} \oint d^n x \operatorname{tr} (D_i E_i W_{\nu\mu\sigma\rho})\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle Q(w) = \oint d^n xyz \dots n \operatorname{tr}(\pi \cdot \delta A \cdot B) = \frac{1}{g^n} \oint d^n xyz \dots n \operatorname{tr} \left(E_j + \frac{\theta g^{\nu\mu\sigma\rho}}{16\pi^{\nu\mu\sigma\rho}} B_j \right) D_{j,w} \\ &= -\frac{1}{g^{\nu\mu\sigma\rho}} \oint d^n x \operatorname{tr} (D_j E_j W_{\nu\mu\sigma\rho})\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle Q(w) = \oint d^n xyz \dots n \operatorname{tr}(\pi \cdot \delta A \cdot B) = \frac{1}{g^n} \oint d^n xyz \dots n \operatorname{tr} \left(E_{i,j} + \frac{\theta g^{\nu\mu\sigma\rho}}{16\pi^{\nu\mu\sigma\rho}} B_{i,j} \right) D_{i,j,w} \\ &= -\frac{1}{g^{\nu\mu\sigma\rho}} \oint d^n x \operatorname{tr} (D_{i,j} E_{i,j} W_{\nu\mu\sigma\rho})\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle Q(w) = \oint d^n xyz \dots n \operatorname{tr}(\pi \cdot \delta A \cdot B) = \frac{1}{g^n} \oint d^n xyz \dots n \operatorname{tr} \left(E_{j,i} + \frac{\theta g^{\nu\mu\sigma\rho}}{16\pi^{\nu\mu\sigma\rho}} B_{j,i} \right) D_{j,i,w} \\ &= -\frac{1}{g^{\nu\mu\sigma\rho}} \oint d^n x \operatorname{tr} (D_{j,i} E_{j,i} W_{\nu\mu\sigma\rho})\end{aligned}$$

m. Función Chern – Simons.

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle D_i(-i \delta\psi/\delta A_i) = \xi_{\lambda\Omega\psi}^{\sigma\zeta\zeta} \int \int \int \int \hbar \phi \mathfrak{K} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \psi \mathfrak{K} \mathfrak{X} \zeta \pi m c^{\mathbb{R}^4}$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle D_j(-j \delta\psi/\delta A_j) = \xi_{\lambda\Omega\psi}^{\sigma\zeta\zeta} \int \int \int \int \hbar \phi \mathfrak{K} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \psi \mathfrak{K} \mathfrak{X} \zeta \pi m c^{\mathbb{R}^4}$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle D_{i,j}(-i \delta\psi/\delta A_{i,j}) = \xi_{\lambda\Omega\psi}^{\sigma\zeta\zeta} \int \int \int \int \hbar \phi \mathfrak{K} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \psi \mathfrak{K} \mathfrak{X} \zeta \pi m c^{\mathbb{R}^4}$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle D_{j,i}(-i \delta\psi/\delta A_{j,i}) = \xi_{\lambda\Omega\psi}^{\sigma\zeta\zeta} \int \int \int \int \hbar \phi \mathfrak{K} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \psi \mathfrak{K} \mathfrak{X} \zeta \pi m c^{\mathbb{R}^4}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle H\psi = g^{\mu\nu\rho\sigma} \operatorname{tr} \left(-i \delta/\delta A - \frac{\theta g^{\mu\nu\rho\sigma}}{16\pi^{\mu\nu\rho\sigma}} B \right) \exp^{\mu\nu\rho\sigma} \psi + 1/g^{\mu\nu\rho\sigma} \operatorname{tr} B^{\mu\nu\rho\sigma} \psi \\ &= \xi_{\lambda\Omega\psi}^{\sigma\zeta\zeta} \int \int \int \int \hbar \phi \mathfrak{K} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \psi \mathfrak{K} \mathfrak{X} \zeta \pi m c^{\mathbb{R}^4}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle H\psi = g^{\mu\nu\rho\sigma} \operatorname{tr} \left(-j \delta/\delta A - \frac{\theta g^{\mu\nu\rho\sigma}}{16\pi^{\mu\nu\rho\sigma}} B \right) \exp^{\mu\nu\rho\sigma} \psi + 1/g^{\mu\nu\rho\sigma} \operatorname{tr} B^{\mu\nu\rho\sigma} \psi \\ &= \xi_{\lambda\Omega\psi}^{\sigma\zeta\zeta} \int \int \int \int \hbar \phi \mathfrak{K} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \psi \mathfrak{K} \mathfrak{X} \zeta \pi m c^{\mathbb{R}^4}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle H\psi = g^{\mu\nu\rho\sigma} \operatorname{tr} \left(-i, j \delta/\delta A - \frac{\theta g^{\mu\nu\rho\sigma}}{16\pi^{\mu\nu\rho\sigma}} B \right) \exp^{\mu\nu\rho\sigma} \psi + 1/g^{\mu\nu\rho\sigma} \operatorname{tr} B^{\mu\nu\rho\sigma} \psi \\ &= \xi_{\lambda\Omega\psi}^{\sigma\zeta\zeta} \int \int \int \int \hbar \phi \mathfrak{K} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \psi \mathfrak{K} \mathfrak{X} \zeta \pi m c^{\mathbb{R}^4}\end{aligned}$$



$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle H\psi = g^{\mu\nu\rho\sigma} \text{tr}(-j, i \delta/\delta A - \frac{\theta g^{\mu\nu\rho\sigma}}{16\pi^{\mu\nu\rho\sigma}} B) \exp^{\mu\nu\rho\sigma} \psi + 1/g^{\mu\nu\rho\sigma} \text{tr} B^{\mu\nu\rho\sigma} \psi \\ &= \xi_{\lambda\Omega\psi}^{\sigma\zeta\zeta} \sum \int \int \int \int \hbar \phi \text{B} \mathfrak{K} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \psi \mathfrak{K} \mathfrak{X} \zeta \pi m c^{\mathbb{R}^4}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle H\psi = g^{\nu\mu\sigma\rho} \text{tr}(-i \delta/\delta A - \frac{\theta g^{\nu\mu\sigma\rho}}{16\pi^{\nu\mu\sigma\rho}} B) \exp^{\nu\mu\sigma\rho} \psi + 1/g^{\nu\mu\sigma\rho} \text{tr} B^{\nu\mu\sigma\rho} \psi \\ &= \xi_{\lambda\Omega\psi}^{\sigma\zeta\zeta} \sum \int \int \int \int \hbar \phi \text{B} \mathfrak{K} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \psi \mathfrak{K} \mathfrak{X} \zeta \pi m c^{\mathbb{R}^4}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle H\psi = g^{\nu\mu\sigma\rho} \text{tr}(-j \delta/\delta A - \frac{\theta g^{\nu\mu\sigma\rho}}{16\pi^{\nu\mu\sigma\rho}} B) \exp^{\nu\mu\sigma\rho} \psi + 1/g^{\nu\mu\sigma\rho} \text{tr} B^{\nu\mu\sigma\rho} \psi \\ &= \xi_{\lambda\Omega\psi}^{\sigma\zeta\zeta} \sum \int \int \int \int \hbar \phi \text{B} \mathfrak{K} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \psi \mathfrak{K} \mathfrak{X} \zeta \pi m c^{\mathbb{R}^4}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle H\psi = g^{\nu\mu\sigma\rho} \text{tr}(-i, j \delta/\delta A - \frac{\theta g^{\nu\mu\sigma\rho}}{16\pi^{\nu\mu\sigma\rho}} B) \exp^{\nu\mu\sigma\rho} \psi + 1/g^{\nu\mu\sigma\rho} \text{tr} B^{\nu\mu\sigma\rho} \psi \\ &= \xi_{\lambda\Omega\psi}^{\sigma\zeta\zeta} \sum \int \int \int \int \hbar \phi \text{B} \mathfrak{K} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \psi \mathfrak{K} \mathfrak{X} \zeta \pi m c^{\mathbb{R}^4}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle H\psi = g^{\nu\mu\sigma\rho} \text{tr}(-j, i \delta/\delta A - \frac{\theta g^{\nu\mu\sigma\rho}}{16\pi^{\nu\mu\sigma\rho}} B) \exp^{\nu\mu\sigma\rho} \psi + 1/g^{\nu\mu\sigma\rho} \text{tr} B^{\nu\mu\sigma\rho} \psi \\ &= \xi_{\lambda\Omega\psi}^{\sigma\zeta\zeta} \sum \int \int \int \int \hbar \phi \text{B} \mathfrak{K} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \psi \mathfrak{K} \mathfrak{X} \zeta \pi m c^{\mathbb{R}^4}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle - g^{\mu\nu\rho\sigma} \text{tr} \delta^{\mu\nu\rho\sigma} \psi_{\mu\nu\rho\sigma} / \delta A + 1/g^{\mu\nu\rho\sigma} \text{tr} B^{\mu\nu\rho\sigma} \psi_{\mu\nu\rho\sigma} \\ &= \xi_{\lambda\Omega\psi}^{\sigma\zeta\zeta} \sum \int \int \int \int \hbar \phi \text{B} \mathfrak{K} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \psi \mathfrak{K} \mathfrak{X} \zeta \pi m c^{\mathbb{R}^4}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle - g^{\nu\mu\sigma\rho} \text{tr} \delta^{\nu\mu\sigma\rho} \psi_{\nu\mu\sigma\rho} / \delta A + 1/g^{\nu\mu\sigma\rho} \text{tr} B^{\nu\mu\sigma\rho} \psi_{\nu\mu\sigma\rho} \\ &= \xi_{\lambda\Omega\psi}^{\sigma\zeta\zeta} \sum \int \int \int \int \hbar \phi \text{B} \mathfrak{K} \mathfrak{Z} \mathfrak{K} \mathfrak{D} \mathfrak{K} \psi \mathfrak{K} \mathfrak{X} \zeta \pi m c^{\mathbb{R}^4}\end{aligned}$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle W(A) = 1/16\pi^{\mu\nu\rho\sigma} \int d^{\mu\nu\rho\sigma} \epsilon^{ijk} \text{tr} (F_{ij} A_k + 2i/3 A_i A_j A_k)$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle W(A) = 1/16\pi^{\mu\nu\rho\sigma} \int d^{\mu\nu\rho\sigma} \epsilon^{jik} \text{tr} (F_{ji} A_k + 2i/3 A_j A_i A_k)$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle W(A) = 1/16\pi^{\mu\nu\rho\sigma} \int d^{\mu\nu\rho\sigma} \epsilon^{kij} \text{tr} (F_k A_{ij} + 2i/3 A_k A_i A_j)$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle W(A) = 1/16\pi^{\mu\nu\rho\sigma} \int d^{\mu\nu\rho\sigma} \epsilon^{kji} \text{tr} (F_k A_{ji} + 2i/3 A_k A_j A_i)$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle W(A) = 1/16\pi^{\mu\nu\rho\sigma} \int d^{\mu\nu\rho\sigma} \epsilon^{ikj} \text{tr} (F_{ik} A_j + 2i/3 A_i A_k A_j)$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle W(A) = 1/16\pi^{\mu\nu\rho\sigma} \int d^{\mu\nu\rho\sigma} \epsilon^{jki} \text{tr} (F_{jk} A_i + 2i/3 A_j A_k A_i)$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle W(A) = 1/16\pi^{\nu\mu\sigma\rho} \int d^{\nu\mu\sigma\rho} \epsilon^{ijk} \text{tr} (F_{ij} A_k + 2i/3 A_i A_j A_k)$$



$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle W(A) = 1/16\pi^{\nu\mu\sigma\rho} \int d^{\nu\mu\sigma\rho} \epsilon^{jik} \text{tr} (F_{ji} A_k + 2i/3 A_j A_i A_k)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle W(A) = 1/16\pi^{\nu\mu\sigma\rho} \int d^{\nu\mu\sigma\rho} \epsilon^{kij} \text{tr} (F_k A_{ij} + 2i/3 A_k A_i A_j)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle W(A) = 1/16\pi^{\nu\mu\sigma\rho} \int d^{\nu\mu\sigma\rho} \epsilon^{kji} \text{tr} (F_k A_{ji} + 2i/3 A_k A_j A_i)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle W(A) = 1/16\pi^{\nu\mu\sigma\rho} \int d^{\nu\mu\sigma\rho} \epsilon^{ikj} \text{tr} (F_{ik} A_j + 2i/3 A_i A_k A_j)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle W(A) = 1/16\pi^{\nu\mu\sigma\rho} \int d^{\nu\mu\sigma\rho} \epsilon^{jki} \text{tr} (F_{jk} A_i + 2i/3 A_j A_k A_i)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_i = 1/16\pi^{\mu\nu\rho\sigma} \epsilon^{ijk} F_{jk} = 1/16\pi^{\mu\nu\rho\sigma} B_i$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_j = 1/16\pi^{\mu\nu\rho\sigma} \epsilon^{ijk} F_{jk} = 1/16\pi^{\mu\nu\rho\sigma} B_j$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_{i,j} = 1/16\pi^{\mu\nu\rho\sigma} \epsilon^{ijk} F_{jk} = 1/16\pi^{\mu\nu\rho\sigma} B_{i,j}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_{j,i} = 1/16\pi^{\mu\nu\rho\sigma} \epsilon^{ijk} F_{jk} = 1/16\pi^{\mu\nu\rho\sigma} B_{j,i}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_i = 1/16\pi^{\mu\nu\rho\sigma} \epsilon^{ikj} F_{kj} = 1/16\pi^{\mu\nu\rho\sigma} B_i$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_j = 1/16\pi^{\mu\nu\rho\sigma} \epsilon^{jki} F_{ki} = 1/16\pi^{\mu\nu\rho\sigma} B_j$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_{i,j} = 1/16\pi^{\mu\nu\rho\sigma} \epsilon^{kij} F_{kj} = 1/16\pi^{\mu\nu\rho\sigma} B_{i,j}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_{j,i} = 1/16\pi^{\mu\nu\rho\sigma} \epsilon^{kji} F_{ki} = 1/16\pi^{\mu\nu\rho\sigma} B_{j,i}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_i = 1/16\pi^{\nu\mu\sigma\rho} \epsilon^{ijk} F_{jk} = 1/16\pi^{\nu\mu\sigma\rho} B_i$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_j = 1/16\pi^{\nu\mu\sigma\rho} \epsilon^{ijk} F_{jk} = 1/16\pi^{\nu\mu\sigma\rho} B_j$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_{i,j} = 1/16\pi^{\nu\mu\sigma\rho} \epsilon^{ijk} F_{jk} = 1/16\pi^{\nu\mu\sigma\rho} B_{i,j}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_{j,i} = 1/16\pi^{\nu\mu\sigma\rho} \epsilon^{ijk} F_{jk} = 1/16\pi^{\nu\mu\sigma\rho} B_{j,i}$$

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$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_j = 1/16\pi^{\nu\mu\sigma\rho} \epsilon^{jki} F_{ki} = 1/16\pi^{\nu\mu\sigma\rho} B_j$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_{i,j} = 1/16\pi^{\nu\mu\sigma\rho} \epsilon^{kij} F_{kj} = 1/16\pi^{\nu\mu\sigma\rho} B_{i,j}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle SW(A) / \delta A_{j,i} = 1/16\pi^{\nu\mu\sigma\rho} \epsilon^{kji} F_{ki} = 1/16\pi^{\nu\mu\sigma\rho} B_{j,i}$$



$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle - i \delta \psi(A)/\delta A_i = -ie^{i\theta W[A]} \frac{\delta \psi_{\mu\nu\sigma\rho}(A)}{\delta A_i} + \frac{\theta}{16\pi^{\mu\nu\sigma\rho}} B_i \psi(A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle - j \delta \psi(A)/\delta A_j = -je^{j\theta W[A]} \frac{\delta \psi_{\mu\nu\sigma\rho}(A)}{\delta A_j} + \frac{\theta}{16\pi^{\mu\nu\sigma\rho}} B_j \psi(A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle - i, j \delta \psi(A)/\delta A_{i,j} = -i, je^{i,j\theta W[A]} \frac{\delta \psi_{\mu\nu\sigma\rho}(A)}{\delta A_{i,j}} + \frac{\theta}{16\pi^{\mu\nu\sigma\rho}} B_{i,j} \psi(A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle - j, i \delta \psi(A)/\delta A_{j,i} = -j, ie^{j,i\theta W[A]} \frac{\delta \psi_{\mu\nu\sigma\rho}(A)}{\delta A_{j,i}} + \frac{\theta}{16\pi^{\mu\nu\sigma\rho}} B_{j,i} \psi(A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle - i \delta \psi(A)/\delta A_i = -ie^{i\theta W[A]} \frac{\delta \psi_{\nu\mu\sigma\rho}(A)}{\delta A_i} + \frac{\theta}{16\pi^{\nu\mu\sigma\rho}} B_i \psi(A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle - j \delta \psi(A)/\delta A_j = -je^{j\theta W[A]} \frac{\delta \psi_{\nu\mu\sigma\rho}(A)}{\delta A_j} + \frac{\theta}{16\pi^{\nu\mu\sigma\rho}} B_j \psi(A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle - i, j \delta \psi(A)/\delta A_{i,j} = -i, je^{i,j\theta W[A]} \frac{\delta \psi_{\nu\mu\sigma\rho}(A)}{\delta A_{i,j}} + \frac{\theta}{16\pi^{\nu\mu\sigma\rho}} B_{i,j} \psi(A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle - j, i \delta \psi(A)/\delta A_{j,i} = -j, ie^{j,i\theta W[A]} \frac{\delta \psi_{\nu\mu\sigma\rho}(A)}{\delta A_{j,i}} + \frac{\theta}{16\pi^{\nu\mu\sigma\rho}} B_{j,i} \psi(A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle W[A]$$

$$\begin{aligned} &\rightarrow W[B] + 1/16\pi^{\mu\nu\sigma\rho} \int d^{\mu\nu\sigma\rho} x [i\epsilon^{ijk} \partial_i \text{tr} (\partial_j \Omega \Omega \Delta \nabla \lambda_{k,i}) n^{-\Omega^{-\mu\nu\sigma\rho}} \\ &- 1/3\epsilon^{ijk} \text{tr} (\Omega^{-\mu\nu\sigma\rho} \partial_i \Omega \Omega^{-\mu\nu\sigma\rho} \partial_j \Omega \Omega^{-\mu\nu\sigma\rho} \partial_k \Omega \Omega^{-\mu\nu\sigma\rho})] \end{aligned}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle W[A]$$

$$\begin{aligned} &\rightarrow W[B] + 1/16\pi^{\mu\nu\sigma\rho} \int d^{\mu\nu\sigma\rho} x [j\epsilon^{ijk} \partial_j \text{tr} (\partial_i \Omega \Omega \Delta \nabla \lambda_{k,j}) n^{-\Omega^{-\mu\nu\sigma\rho}} \\ &- 1/3\epsilon^{ijk} \text{tr} (\Omega^{-\mu\nu\sigma\rho} \partial_j \Omega \Omega^{-\mu\nu\sigma\rho} \partial_i \Omega \Omega^{-\mu\nu\sigma\rho} \partial_k \Omega \Omega^{-\mu\nu\sigma\rho})] \end{aligned}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle W[A]$$

$$\begin{aligned} &\rightarrow W[B] + 1/16\pi^{\mu\nu\sigma\rho} \int d^{\mu\nu\sigma\rho} x [i\epsilon^{ijk} \partial_i \text{tr} (\partial_j \Omega \Omega \Delta \nabla \lambda_{i,k}) n^{-\Omega^{-\mu\nu\sigma\rho}} \\ &- 1/3\epsilon^{ijk} \text{tr} (\Omega^{-\mu\nu\sigma\rho} \partial_i \Omega \Omega^{-\mu\nu\sigma\rho} \partial_j \Omega \Omega^{-\mu\nu\sigma\rho} \partial_k \Omega \Omega^{-\mu\nu\sigma\rho})] \end{aligned}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle W[A]$$

$$\begin{aligned} &\rightarrow W[B] + 1/16\pi^{\mu\nu\sigma\rho} \int d^{\mu\nu\sigma\rho} x [j\epsilon^{ijk} \partial_j \text{tr} (\partial_i \Omega \Omega \Delta \nabla \lambda_{j,k}) n^{-\Omega^{-\mu\nu\sigma\rho}} \\ &- 1/3\epsilon^{ijk} \text{tr} (\Omega^{-\mu\nu\sigma\rho} \partial_j \Omega \Omega^{-\mu\nu\sigma\rho} \partial_i \Omega \Omega^{-\mu\nu\sigma\rho} \partial_k \Omega \Omega^{-\mu\nu\sigma\rho})] \end{aligned}$$



$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{\mu\nu\sigma\rho} \int d^{\mu\nu\sigma\rho} x[j\epsilon^{jki}\partial_j \text{tr}(\partial_i\Omega\Omega\Delta\nabla\lambda_{j,k})n^{-\Omega^{-\mu\nu\sigma\rho}} \\ &\quad - 1/3\epsilon^{jki} \text{tr}(\Omega^{-\mu\nu\sigma\rho}\partial_j\Omega\Omega^{-\mu\nu\sigma\rho}\partial_i\Omega\Omega^{-\mu\nu\sigma\rho}\partial_k\Omega\Omega^{-\mu\nu\sigma\rho})\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{\mu\nu\sigma\rho} \int d^{\mu\nu\sigma\rho} x[i\epsilon^{jki}\partial_i \text{tr}(\partial_j\Omega\Omega\Delta\nabla\lambda_{i,k})n^{-\Omega^{-\mu\nu\sigma\rho}} \\ &\quad - 1/3\epsilon^{jki} \text{tr}(\Omega^{-\mu\nu\sigma\rho}\partial_i\Omega\Omega^{-\mu\nu\sigma\rho}\partial_j\Omega\Omega^{-\mu\nu\sigma\rho}\partial_k\Omega\Omega^{-\mu\nu\sigma\rho})\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{\mu\nu\sigma\rho} \int d^{\mu\nu\sigma\rho} x[k\epsilon^{jki}\partial_k \text{tr}(\partial_k\Omega\Omega\Delta\nabla\lambda_{j,i})n^{-\Omega^{-\mu\nu\sigma\rho}} \\ &\quad - 1/3\epsilon^{jki} \text{tr}(\Omega^{-\mu\nu\sigma\rho}\partial_k\Omega\Omega^{-\mu\nu\sigma\rho}\partial_j\Omega\Omega^{-\mu\nu\sigma\rho}\partial_i\Omega\Omega^{-\mu\nu\sigma\rho})\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{\mu\nu\sigma\rho} \int d^{\mu\nu\sigma\rho} x[k\epsilon^{jki}\partial_k \text{tr}(\partial_k\Omega\Omega\Delta\nabla\lambda_{i,j})n^{-\Omega^{-\mu\nu\sigma\rho}} \\ &\quad - 1/3\epsilon^{jki} \text{tr}(\Omega^{-\mu\nu\sigma\rho}\partial_k\Omega\Omega^{-\mu\nu\sigma\rho}\partial_i\Omega\Omega^{-\mu\nu\sigma\rho}\partial_j\Omega\Omega^{-\mu\nu\sigma\rho})\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{\mu\nu\sigma\rho} \int d^{\mu\nu\sigma\rho} x[i\epsilon^{kij}\partial_i \text{tr}(\partial_j\Omega\Omega\Delta\nabla\lambda_{k,i})n^{-\Omega^{-\mu\nu\sigma\rho}} \\ &\quad - 1/3\epsilon^{kij} \text{tr}(\Omega^{-\mu\nu\sigma\rho}\partial_i\Omega\Omega^{-\mu\nu\sigma\rho}\partial_j\Omega\Omega^{-\mu\nu\sigma\rho}\partial_k\Omega\Omega^{-\mu\nu\sigma\rho})\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{\mu\nu\sigma\rho} \int d^{\mu\nu\sigma\rho} x[j\epsilon^{kij}\partial_j \text{tr}(\partial_i\Omega\Omega\Delta\nabla\lambda_{k,j})n^{-\Omega^{-\mu\nu\sigma\rho}} \\ &\quad - 1/3\epsilon^{kij} \text{tr}(\Omega^{-\mu\nu\sigma\rho}\partial_j\Omega\Omega^{-\mu\nu\sigma\rho}\partial_i\Omega\Omega^{-\mu\nu\sigma\rho}\partial_k\Omega\Omega^{-\mu\nu\sigma\rho})\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{\mu\nu\sigma\rho} \int d^{\mu\nu\sigma\rho} x[i\epsilon^{kij}\partial_i \text{tr}(\partial_j\Omega\Omega\Delta\nabla\lambda_{i,k})n^{-\Omega^{-\mu\nu\sigma\rho}} \\ &\quad - 1/3\epsilon^{kij} \text{tr}(\Omega^{-\mu\nu\sigma\rho}\partial_i\Omega\Omega^{-\mu\nu\sigma\rho}\partial_j\Omega\Omega^{-\mu\nu\sigma\rho}\partial_k\Omega\Omega^{-\mu\nu\sigma\rho})\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{\mu\nu\sigma\rho} \int d^{\mu\nu\sigma\rho} x[j\epsilon^{kij}\partial_j \text{tr}(\partial_i\Omega\Omega\Delta\nabla\lambda_{j,k})n^{-\Omega^{-\mu\nu\sigma\rho}} \\ &\quad - 1/3\epsilon^{kij} \text{tr}(\Omega^{-\mu\nu\sigma\rho}\partial_j\Omega\Omega^{-\mu\nu\sigma\rho}\partial_i\Omega\Omega^{-\mu\nu\sigma\rho}\partial_k\Omega\Omega^{-\mu\nu\sigma\rho})\end{aligned}$$



$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{v\mu\rho\sigma} \int d^{v\mu\rho\sigma} x [j\epsilon^{jik} \partial_j \text{tr} (\partial_i \Omega \Omega \Delta \nabla \lambda_{i,k}) n^{-\Omega^{-v\mu\rho\sigma}} \\ &\quad - 1/3\epsilon^{jik} \text{tr} (\Omega^{-v\mu\rho\sigma} \partial_j \Omega \Omega^{-v\mu\rho\sigma} \partial_i \Omega \Omega^{-v\mu\rho\sigma} \partial_k \Omega \Omega^{-v\mu\rho\sigma})]\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{v\mu\rho\sigma} \int d^{v\mu\rho\sigma} x [i\epsilon^{jik} \partial_i \text{tr} (\partial_j \Omega \Omega \Delta \nabla \lambda_{j,k}) n^{-\Omega^{-v\mu\rho\sigma}} \\ &\quad - 1/3\epsilon^{jik} \text{tr} (\Omega^{-v\mu\rho\sigma} \partial_i \Omega \Omega^{-v\mu\rho\sigma} \partial_j \Omega \Omega^{-v\mu\rho\sigma} \partial_k \Omega \Omega^{-v\mu\rho\sigma})]\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{v\mu\rho\sigma} \int d^{v\mu\rho\sigma} x [k\epsilon^{jik} \partial_k \text{tr} (\partial_k \Omega \Omega \Delta \nabla \lambda_{j,i}) n^{-\Omega^{-v\mu\rho\sigma}} \\ &\quad - 1/3\epsilon^{jik} \text{tr} (\Omega^{-v\mu\rho\sigma} \partial_k \Omega \Omega^{-v\mu\rho\sigma} \partial_j \Omega \Omega^{-v\mu\rho\sigma} \partial_i \Omega \Omega^{-v\mu\rho\sigma})]\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{v\mu\rho\sigma} \int d^{v\mu\rho\sigma} x [k\epsilon^{jik} \partial_k \text{tr} (\partial_k \Omega \Omega \Delta \nabla \lambda_{i,j}) n^{-\Omega^{-v\mu\rho\sigma}} \\ &\quad - 1/3\epsilon^{jik} \text{tr} (\Omega^{-v\mu\rho\sigma} \partial_k \Omega \Omega^{-v\mu\rho\sigma} \partial_i \Omega \Omega^{-v\mu\rho\sigma} \partial_j \Omega \Omega^{-v\mu\rho\sigma})]\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{v\mu\rho\sigma} \int d^{v\mu\rho\sigma} x [i\epsilon^{ikj} \partial_i \text{tr} (\partial_j \Omega \Omega \Delta \nabla \lambda_{k,i}) n^{-\Omega^{-v\mu\rho\sigma}} \\ &\quad - 1/3\epsilon^{ikj} \text{tr} (\Omega^{-v\mu\rho\sigma} \partial_i \Omega \Omega^{-v\mu\rho\sigma} \partial_j \Omega \Omega^{-v\mu\rho\sigma} \partial_k \Omega \Omega^{-v\mu\rho\sigma})]\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{v\mu\rho\sigma} \int d^{v\mu\rho\sigma} x [j\epsilon^{ikj} \partial_j \text{tr} (\partial_i \Omega \Omega \Delta \nabla \lambda_{k,j}) n^{-\Omega^{-v\mu\rho\sigma}} \\ &\quad - 1/3\epsilon^{ikj} \text{tr} (\Omega^{-v\mu\rho\sigma} \partial_j \Omega \Omega^{-v\mu\rho\sigma} \partial_i \Omega \Omega^{-v\mu\rho\sigma} \partial_k \Omega \Omega^{-v\mu\rho\sigma})]\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{v\mu\rho\sigma} \int d^{v\mu\rho\sigma} x [i\epsilon^{ikj} \partial_i \text{tr} (\partial_j \Omega \Omega \Delta \nabla \lambda_{i,k}) n^{-\Omega^{-v\mu\rho\sigma}} \\ &\quad - 1/3\epsilon^{ikj} \text{tr} (\Omega^{-v\mu\rho\sigma} \partial_i \Omega \Omega^{-v\mu\rho\sigma} \partial_j \Omega \Omega^{-v\mu\rho\sigma} \partial_k \Omega \Omega^{-v\mu\rho\sigma})]\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle W[A] \\ &\rightarrow W[B] + 1/16\pi^{v\mu\rho\sigma} \int d^{v\mu\rho\sigma} x [j\epsilon^{ikj} \partial_j \text{tr} (\partial_i \Omega \Omega \Delta \nabla \lambda_{j,k}) n^{-\Omega^{-v\mu\rho\sigma}} \\ &\quad - 1/3\epsilon^{ikj} \text{tr} (\Omega^{-v\mu\rho\sigma} \partial_j \Omega \Omega^{-v\mu\rho\sigma} \partial_i \Omega \Omega^{-v\mu\rho\sigma} \partial_k \Omega \Omega^{-v\mu\rho\sigma})]\end{aligned}$$



$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle n(\Omega) = 1/32\pi^{\nu\mu\rho\sigma} \int_{S^3} d^{\nu\mu\rho\sigma} S \epsilon^{kji} \text{tr}(\Omega^{-\nu\mu\rho\sigma} \partial_k \Omega \Omega^{-\nu\mu\rho\sigma} \partial_j \Omega \Omega^{-\nu\mu\rho\sigma} \partial_i \Omega \Omega^{-\nu\mu\rho\sigma})$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \psi(A) = e^{i\theta W[A]} \psi_0(A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \psi(B) = e^{i\theta W[B]} \psi_0(B)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \psi(\partial\Delta\nabla\omega) = e^{i\theta W[\partial\Delta\nabla\omega]} \psi_\phi \psi \partial\Delta\nabla\vartheta\varphi\tau(A)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \psi(\partial\Delta\nabla\omega) = e^{i\theta W[\partial\Delta\nabla\omega]} \psi_\phi \psi \partial\Delta\nabla\vartheta\varphi\tau(B)$$

n. Dinámica hamiltoniana de partículas según la teoría de Yang-Mills.

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle = 1/\pi\epsilon^{ijk} e^{i\theta W[\partial\Delta\nabla\omega]} (-i\partial/\partial x + \Phi/\partial\pi R) \exp^{\mu\nu\rho\sigma} + \psi_\phi \psi \partial\Delta\nabla\vartheta\varphi\tau(A) + \psi =$$

$$\frac{1}{\nu\mu\rho\sigma \sqrt{\frac{1}{\pi\epsilon^{ijk}} e^{\frac{i\theta W[\partial\Delta\nabla\omega]}{R}}}} = E = \frac{1}{\pi e R^2} (n + \frac{\phi}{2\pi\varphi}) = \xi_{\lambda\Omega\psi}^{\sigma\sigma\zeta} \sum \int \int \int \int \hbar \phi \text{bK} \tilde{\text{Z}} \text{K} \text{DK} \psi \text{K} \text{X} \zeta \pi m c^{\mathbb{R}^4}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle = 1/\pi\epsilon^{ijk} e^{i\theta W[\partial\Delta\nabla\omega]} (-i\partial/\partial x + \Phi/\partial\pi R) \exp^{\nu\mu\rho\sigma} + \psi_\phi \psi \partial\Delta\nabla\vartheta\varphi\tau(A) + \psi =$$

$$\frac{1}{\nu\mu\rho\sigma \sqrt{\frac{1}{\pi\epsilon^{ijk}} e^{\frac{i\theta W[\partial\Delta\nabla\omega]}{R}}}} = E = \frac{1}{\pi e R^2} (n + \frac{\phi}{2\pi\varphi}) = \xi_{\lambda\Omega\psi}^{\sigma\sigma\zeta} \sum \int \int \int \int \hbar \phi \text{bK} \tilde{\text{Z}} \text{K} \text{DK} \psi \text{K} \text{X} \zeta \pi m c^{\mathbb{R}^4}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle = 1/\pi\epsilon^{ijk} e^{i\theta W[\partial\Delta\nabla\omega]} (-i\partial/\partial x + \Phi/\partial\pi R) \exp^{\mu\nu\rho\sigma} + \psi_\phi \psi \partial\Delta\nabla\vartheta\varphi\tau(B) + \psi =$$

$$\frac{1}{\nu\mu\rho\sigma \sqrt{\frac{1}{\pi\epsilon^{ijk}} e^{\frac{i\theta W[\partial\Delta\nabla\omega]}{R}}}} = E = \frac{1}{\pi e R^2} (n + \frac{\phi}{2\pi\varphi}) = \xi_{\lambda\Omega\psi}^{\sigma\sigma\zeta} \sum \int \int \int \int \hbar \phi \text{bK} \tilde{\text{Z}} \text{K} \text{DK} \psi \text{K} \text{X} \zeta \pi m c^{\mathbb{R}^4}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle = 1/\pi\epsilon^{ijk} e^{i\theta W[\partial\Delta\nabla\omega]} (-i\partial/\partial x + \Phi/\partial\pi R) \exp^{\nu\mu\rho\sigma} + \psi_\phi \psi \partial\Delta\nabla\vartheta\varphi\tau(B) + \psi =$$

$$\frac{1}{\nu\mu\rho\sigma \sqrt{\frac{1}{\pi\epsilon^{ijk}} e^{\frac{i\theta W[\partial\Delta\nabla\omega]}{R}}}} = E = \frac{1}{\pi e R^2} (n + \frac{\phi}{2\pi\varphi}) = \xi_{\lambda\Omega\psi}^{\sigma\sigma\zeta} \sum \int \int \int \int \hbar \phi \text{bK} \tilde{\text{Z}} \text{K} \text{DK} \psi \text{K} \text{X} \zeta \pi m c^{\mathbb{R}^4}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle = 1/\pi\epsilon^{ikj} e^{i\theta W[\partial\Delta\nabla\omega]} (-i\partial/\partial x + \Phi/\partial\pi R) \exp^{\mu\nu\rho\sigma} + \psi_\phi \psi \partial\Delta\nabla\vartheta\varphi\tau(A) + \psi =$$

$$\frac{1}{\nu\mu\rho\sigma \sqrt{\frac{1}{\pi\epsilon^{ikj}} e^{\frac{i\theta W[\partial\Delta\nabla\omega]}{R}}}} = E = \frac{1}{\pi e R^2} (n + \frac{\phi}{2\pi\varphi}) = \xi_{\lambda\Omega\psi}^{\sigma\sigma\zeta} \sum \int \int \int \int \hbar \phi \text{bK} \tilde{\text{Z}} \text{K} \text{DK} \psi \text{K} \text{X} \zeta \pi m c^{\mathbb{R}^4}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle = 1/\pi\epsilon^{ikj} e^{i\theta W[\partial\Delta\nabla\omega]} (-i\partial/\partial x + \Phi/\partial\pi R) \exp^{\nu\mu\rho\sigma} + \psi_\phi \psi \partial\Delta\nabla\vartheta\varphi\tau(A) + \psi =$$

$$\frac{1}{\nu\mu\rho\sigma \sqrt{\frac{1}{\pi\epsilon^{ikj}} e^{\frac{i\theta W[\partial\Delta\nabla\omega]}{R}}}} = E = \frac{1}{\pi e R^2} (n + \frac{\phi}{2\pi\varphi}) = \xi_{\lambda\Omega\psi}^{\sigma\sigma\zeta} \sum \int \int \int \int \hbar \phi \text{bK} \tilde{\text{Z}} \text{K} \text{DK} \psi \text{K} \text{X} \zeta \pi m c^{\mathbb{R}^4}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle = 1/\pi\epsilon^{ikj} e^{i\theta W[\partial\Delta\nabla\omega]} (-i\partial/\partial x + \Phi/\partial\pi R) \exp^{\mu\nu\rho\sigma} + \psi_\phi \psi \partial\Delta\nabla\vartheta\varphi\tau(B) + \psi =$$

$$\frac{1}{\nu\mu\rho\sigma \sqrt{\frac{1}{\pi\epsilon^{ikj}} e^{\frac{i\theta W[\partial\Delta\nabla\omega]}{R}}}} = E = \frac{1}{\pi e R^2} (n + \frac{\phi}{2\pi\varphi}) = \xi_{\lambda\Omega\psi}^{\sigma\sigma\zeta} \sum \int \int \int \int \hbar \phi \text{bK} \tilde{\text{Z}} \text{K} \text{DK} \psi \text{K} \text{X} \zeta \pi m c^{\mathbb{R}^4}$$



$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{v\mu\rho\sigma}(B') = e^{kij\theta n} \varphi_{v\mu\rho\sigma}(Bk, Bi, Bj)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{v\mu\rho\sigma}(A') = e^{kji\theta n} \varphi_{v\mu\rho\sigma}(Ak, Aj, Ai)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{v\mu\rho\sigma}(A') = e^{kji\theta n} \varphi_{v\mu\rho\sigma}(Bk, Bj, Bi)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{v\mu\rho\sigma}(B') = e^{kji\theta n} \varphi_{v\mu\rho\sigma}(Ak, Aj, Ai)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{v\mu\rho\sigma}(B') = e^{kji\theta n} \varphi_{v\mu\rho\sigma}(Bk, Bj, Bi)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{i\theta n} \varphi_{v\mu\rho\sigma}(Ai)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{i\theta n} \varphi_{v\mu\rho\sigma}(Bi)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{i\theta n} \varphi_{v\mu\rho\sigma}(Ai)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{i\theta n} \varphi_{v\mu\rho\sigma}(Bi)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{j\theta n} \varphi_{v\mu\rho\sigma}(Aj)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{j\theta n} \varphi_{v\mu\rho\sigma}(Bj)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{j\theta n} \varphi_{v\mu\rho\sigma}(Aj)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{j\theta n} \varphi_{v\mu\rho\sigma}(Bj)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{k\theta n} \varphi_{v\mu\rho\sigma}(Ak)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{k\theta n} \varphi_{v\mu\rho\sigma}(Bk)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{k\theta n} \varphi_{v\mu\rho\sigma}(Ak)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{k\theta n} \varphi_{v\mu\rho\sigma}(Bk)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{ijk\theta n} \varphi_{v\mu\rho\sigma}(Ai, Aj, Ak)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{ijk\theta n} \varphi_{v\mu\rho\sigma}(Bi, Bj, Bk)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{ijk\theta n} \varphi_{v\mu\rho\sigma}(Ai, Aj, Ak)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{ijk\theta n} \varphi_{v\mu\rho\sigma}(Bi, Bj, Bk)$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{ikj\theta n} \varphi_{v\mu\rho\sigma}(Ai, Ak, Aj)$$



$$\begin{aligned}
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{ikj\theta n} \varphi_{\nu\mu\rho\sigma}(Bi, Bk, Bj) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{ikj\theta n} \varphi_{\nu\mu\rho\sigma}(Ai, Ak, Aj) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{ikj\theta n} \varphi_{\nu\mu\rho\sigma}(Bi, Bk, Bj) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{jik\theta n} \varphi_{\nu\mu\rho\sigma}(Aj, Ai, Ak) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{jik\theta n} \varphi_{\nu\mu\rho\sigma}(Bj, Bi, Bk) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{jik\theta n} \varphi_{\nu\mu\rho\sigma}(Aj, Ai, Ak) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{jik\theta n} \varphi_{\nu\mu\rho\sigma}(Bj, Bi, Bk) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{jki\theta n} \varphi_{\nu\mu\rho\sigma}(Aj, Ak, Ai) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{jki\theta n} \varphi_{\nu\mu\rho\sigma}(Bj, Bk, Bi) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{jki\theta n} \varphi_{\nu\mu\rho\sigma}(Aj, Ak, Ai) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{jki\theta n} \varphi_{\nu\mu\rho\sigma}(Bj, Bk, Bi) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{kij\theta n} \varphi_{\nu\mu\rho\sigma}(Ak, Ai, Aj) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{kij\theta n} \varphi_{\nu\mu\rho\sigma}(Bk, Bi, Bj) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{kij\theta n} \varphi_{\nu\mu\rho\sigma}(Ak, Ai, Aj) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{kij\theta n} \varphi_{\nu\mu\rho\sigma}(Bk, Bi, Bj) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{kji\theta n} \varphi_{\nu\mu\rho\sigma}(Ak, Aj, Ai) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(A') = e^{kji\theta n} \varphi_{\nu\mu\rho\sigma}(Bk, Bj, Bi) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{kji\theta n} \varphi_{\nu\mu\rho\sigma}(Ak, Aj, Ai) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\mu\nu\sigma\rho}(B') = e^{kji\theta n} \varphi_{\nu\mu\rho\sigma}(Bk, Bj, Bi) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\nu\mu\rho\sigma}(A') = e^{i\theta n} \varphi_{\mu\nu\sigma\rho}(Ai) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\nu\mu\rho\sigma}(A') = e^{i\theta n} \varphi_{\mu\nu\sigma\rho}(Bi) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\nu\mu\rho\sigma}(B') = e^{i\theta n} \varphi_{\mu\nu\sigma\rho}(Ai)
\end{aligned}$$



$$\begin{aligned}
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\nu\mu\rho\sigma}(A') = e^{jki\theta n} \varphi_{\mu\nu\sigma\rho}(Bj, Bk, Bi) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\nu\mu\rho\sigma}(B') = e^{jki\theta n} \varphi_{\mu\nu\sigma\rho}(Aj, Ak, Ai) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\nu\mu\rho\sigma}(B') = e^{jki\theta n} \varphi_{\mu\nu\sigma\rho}(Bj, Bk, Bi) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\nu\mu\rho\sigma}(A') = e^{kij\theta n} \varphi_{\mu\nu\sigma\rho}(Ak, Ai, Aj) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\nu\mu\rho\sigma}(A') = e^{kij\theta n} \varphi_{\mu\nu\sigma\rho}(Bk, Bi, Bj) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\nu\mu\rho\sigma}(B') = e^{kij\theta n} \varphi_{\mu\nu\sigma\rho}(Ak, Ai, Aj) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\nu\mu\rho\sigma}(B') = e^{kij\theta n} \varphi_{\mu\nu\sigma\rho}(Bk, Bi, Bj) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\nu\mu\rho\sigma}(A') = e^{kji\theta n} \varphi_{\mu\nu\sigma\rho}(Ak, Aj, Ai) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\nu\mu\rho\sigma}(A') = e^{kji\theta n} \varphi_{\mu\nu\sigma\rho}(Bk, Bj, Bi) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\nu\mu\rho\sigma}(B') = e^{kji\theta n} \varphi_{\mu\nu\sigma\rho}(Ak, Aj, Ai) \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \varphi_{\nu\mu\rho\sigma}(B') = e^{kji\theta n} \varphi_{\mu\nu\sigma\rho}(Bk, Bj, Bi)
\end{aligned}$$

p. Ondas de Bloch.

$$\begin{aligned}
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle iV\nabla V^{\mu\nu\sigma\rho} + iV\nabla V^{ijk} + iV\nabla V^{\mu\nu} + iV\nabla V_{\nu u} = \lambda\nabla\Delta_i^j k \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle iV\nabla V^{v\mu\rho\sigma} + iV\nabla V^{ijk} + iV\nabla V^{\mu\nu} + iV\nabla V_{\nu u} = \lambda\nabla\Delta_i^j k \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle iV\nabla V^{\mu\nu\sigma\rho} + iV\nabla V^{ikj} + iV\nabla V^{\mu\nu} + iV\nabla V_{\nu u} = \lambda\nabla\Delta_k^i j \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle iV\nabla V^{v\mu\rho\sigma} + iV\nabla V^{ikj} + iV\nabla V^{\mu\nu} + iV\nabla V_{\nu u} = \lambda\nabla\Delta_k^i j \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle jV\nabla V^{\mu\nu\sigma\rho} + jV\nabla V^{jik} + jV\nabla V^{\mu\nu} + jV\nabla V_{\nu u} = \lambda\nabla\Delta_i^j k \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle iV\nabla V^{v\mu\rho\sigma} + iV\nabla V^{jik} + iV\nabla V^{\mu\nu} + iV\nabla V_{\nu u} = \lambda\nabla\Delta_i^j k \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle iV\nabla V^{\mu\nu\sigma\rho} + iV\nabla V^{jki} + iV\nabla V^{\mu\nu} + iV\nabla V_{\nu u} = \lambda\nabla\Delta_k^j i \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle iV\nabla V^{v\mu\rho\sigma} + iV\nabla V^{jki} + iV\nabla V^{\mu\nu} + iV\nabla V_{\nu u} = \lambda\nabla\Delta_k^j i \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle kV\nabla V^{\mu\nu\sigma\rho} + kV\nabla V^{kij} + kV\nabla V^{\mu\nu} + kV\nabla V_{\nu u} = \lambda\nabla\Delta_i^k j \\
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle iV\nabla V^{v\mu\rho\sigma} + iV\nabla V^{kij} + iV\nabla V^{\mu\nu} + iV\nabla V_{\nu u} = \lambda\nabla\Delta_i^k j
\end{aligned}$$



$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle iV\nabla V^{\mu\nu\sigma\rho} + iV\nabla V^{kji} + iV\nabla V^{\mu\nu} + iV\nabla V_{vu} = \lambda\nabla\Delta_j^k i$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle iV\nabla V^{\nu\mu\rho\sigma} + iV\nabla V^{kji} + iV\nabla V^{\mu\nu} + iV\nabla V_{vu} = \lambda\nabla\Delta_j^k i$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \Omega | \psi \rangle = e^{i\theta n'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega | \psi \rangle = e^{i\theta m'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega | \psi \rangle \\ &= e^{i\theta m', n'} | \psi \rangle \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \Omega | \psi \rangle = e^{j\theta n'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega | \psi \rangle = e^{j\theta m'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega | \psi \rangle \\ &= e^{j\theta m', n'} | \psi \rangle \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \Omega | \psi \rangle = e^{k\theta n'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega | \psi \rangle = e^{k\theta m'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega \\ &| \psi \rangle = e^{k\theta m', n'} | \psi \rangle \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \Omega | \psi \rangle = e^{ijk\theta n'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega | \psi \rangle = e^{ijk\theta m'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega \\ &| \psi \rangle = e^{ijk\theta m', n'} | \psi \rangle \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \Omega | \psi \rangle = e^{ikj\theta n'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega | \psi \rangle = e^{ikj\theta m'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega \\ &| \psi \rangle = e^{ikj\theta m', n'} | \psi \rangle \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \Omega | \psi \rangle = e^{jik\theta n'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega | \psi \rangle = e^{jik\theta m'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega \\ &| \psi \rangle = e^{jik\theta m', n'} | \psi \rangle \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \Omega | \psi \rangle = e^{jki\theta n'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega | \psi \rangle = e^{jki\theta m'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega \\ &| \psi \rangle = e^{jki\theta m', n'} | \psi \rangle \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \Omega | \psi \rangle = e^{kij\theta n'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega | \psi \rangle = e^{kij\theta m'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega \\ &| \psi \rangle = e^{kij\theta m', n'} | \psi \rangle \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \Omega | \psi \rangle = e^{kji\theta n'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega | \psi \rangle = e^{kji\theta m'} | \psi \rangle + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega \\ &| \psi \rangle = e^{kji\theta m', n'} | \psi \rangle \end{aligned}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega | \psi \rangle | \theta \rangle$$

$$\begin{aligned} &= \sum_{\substack{\Delta\mu\nu \\ \nabla\nu\mu}} \lambda_{ijk} \iiint | d_{\nu\mu}^{\mu\nu} tr \rangle^{ijk} \sqrt{\partial e^{i\theta n'} \partial e^{i\theta m'} \partial e^{j\theta n'} \partial e^{j\theta m'} \partial e^{k\theta n'} \partial e^{k\theta m'} \partial e^{ijk\theta} }^\infty | \psi \rangle | n \rangle \\ &| m \rangle | \xi \sigma \mathbb{R}^4 \rangle \end{aligned}$$



q. Instantones.

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle S_\theta = \theta/16\pi^2 \int \int d^{ijk} x \operatorname{tr} * F^{\mu\nu} F_{\nu\mu} = \theta/8\pi^2 \int \int d^{ijk} x \partial_{\mu\nu} K^{\nu\mu} \\ &= e^{\mu\nu\rho\sigma} \operatorname{tr} (A_{\mu\nu} \partial_\rho A_\sigma - 2ijk/3 A_{\mu\nu} \partial_\rho A_\sigma) e^{\nu\mu\sigma\rho} \operatorname{tr} (A_{\nu\mu} \partial_\sigma A_\rho - 2ijk/3 A_{\nu\mu} \partial_\sigma A_\rho)\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle A_{\mu\nu} \mapsto i\Omega \partial_{\mu\nu} \Omega^{-ijk} + \hat{H}|\psi\rangle = E_\psi|\psi\rangle A_{\mu\nu} \mapsto j\Omega \partial_{\mu\nu} \Omega^{-ijk} + \hat{H}|\psi\rangle = E_\psi|\psi\rangle A_{\mu\nu} \\ &\mapsto k\Omega \partial_{\mu\nu} \Omega^{-ijk}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle A_{\nu\mu} \mapsto i\Omega \partial_{\nu\mu} \Omega^{-ijk} + \hat{H}|\psi\rangle = E_\psi|\psi\rangle A_{\nu\mu} \mapsto j\Omega \partial_{\nu\mu} \Omega^{-ijk} + \hat{H}|\psi\rangle = E_\psi|\psi\rangle A_{\nu\mu} \\ &\mapsto k\Omega \partial_{\nu\mu} \Omega^{-ijk}\end{aligned}$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle v(\Omega) = 1/24\pi^2 \oint_{v\mu}^{\mu\nu} S_\infty^{\mu\nu\nu\mu} d^{ijk\mu\nu\nu\mu} S \varepsilon^{ijk} \operatorname{tr} (\Omega \partial_i \Omega^{-i}) (\Omega \partial_j \Omega^{-j}) (\Omega \partial_k \Omega^{-k})$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle S_{YM} = 1/8g^2 \int d^{ijk} x \operatorname{tr} (F_{\mu\nu} \tilde{*} F_{\nu\mu}) \exp^2 \mp 1/4g^2 \int d^{ijk} x \operatorname{tr} F_{\mu\nu} * F^{\nu\mu} \\ &\cong 16\pi^2/g^{ijk} |\mu\nu| \pm |v\mu|\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle S_{YM} = 1/8g^2 \int d^{ijk} x \operatorname{tr} (F_{\nu\mu} \pm * F_{\mu\nu}) \exp^2 \pm 1/4g^2 \int d^{ijk} x \operatorname{tr} F_{\nu\mu} * F^{\mu\nu} \\ &\cong 16\pi^2/g^{ijk} |v\mu| \pm |\mu\nu|\end{aligned}$$

$$\hat{H}|\psi\rangle = E_\psi|\psi\rangle e^{-S_{\text{instanton}}} = e^{\partial^{\pi^2} |\mu\nu| \pm |v\mu|/g^{ijk}} e^{ijk\theta|v\mu| \pm |\mu\nu|}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle \Omega(x) = x_\mu \sigma^\mu / \sqrt{x_\mu^i + A_\mu} \mapsto i\Omega \partial_\mu \Omega^{ijk} = 1/x_{ijk}^\mu \eta_{\mu\nu}^i \sigma^i + A_\mu \\ &= 1/x^{ijk} + \rho^{ijk} \eta_{\mu\nu}^i x^\nu \sigma^i + F_{\mu\nu} = 2\rho^{ijk} / (x^{ijk} + \rho^{ijk}) \exp^{ijk} \eta_{\mu\nu}^i \sigma^i\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle \Omega(y) = y_\mu \sigma^\mu / \sqrt{y_\mu^i + A_\mu} \mapsto i\Omega \partial_\mu \Omega^{ijk} = 1/y_{ijk}^\mu \eta_{\mu\nu}^i \sigma^i + A_\mu \\ &= 1/y^{ijk} + \rho^{ijk} \eta_{\mu\nu}^i y^\nu \sigma^i + F_{\mu\nu} = 2\rho^{ijk} / (y^{ijk} + \rho^{ijk}) \exp^{ijk} \eta_{\mu\nu}^i \sigma^i\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle \Omega(z) = z_\mu \sigma^\mu / \sqrt{z_\mu^i + A_\mu} \mapsto i\Omega \partial_\mu \Omega^{ijk} = 1/z_{ijk}^\mu \eta_{\mu\nu}^i \sigma^i + A_\mu \\ &= 1/z^{ijk} + \rho^{ijk} \eta_{\mu\nu}^i z^\nu \sigma^i + F_{\mu\nu} = 2\rho^{ijk} / (z^{ijk} + \rho^{ijk}) \exp^{ijk} \eta_{\mu\nu}^i \sigma^i\end{aligned}$$

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$$\eta_{\mu i}^1 = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix} \quad \eta_{\mu i}^2 = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ -1 & 0 & 0 \end{pmatrix} \quad \eta_{\mu i}^3 = \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix} \quad \eta_{\mu i}^\infty = \begin{pmatrix} 0 & -1 & 0 \\ 0 & 1 & 1 \\ -1 & 0 & 0 \end{pmatrix}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \Omega(x) = x_\nu \sigma^v / \sqrt{x_\nu^i} + A_\nu \mapsto i\Omega \partial_\nu \Omega^{ijk} = 1/x_{ijk}^v \eta_{\nu\mu}^i \sigma^i + A_\nu \\ &= 1/x^{ijk} + \rho^{ijk} \eta_{\nu\mu}^i x^\mu \sigma^i + F_{\nu\mu} = 2\rho^{ijk} / (x^{ijk} + \rho^{ijk}) \exp^{ijk} \eta_{\nu\mu}^i \sigma^i \end{aligned}$$

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$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \Omega(x) = x_{\mu\nu} \sigma^{\mu\nu} / \sqrt{x_{\mu\nu}^{ijk}} + A_{\mu\nu} \mapsto ijk\Omega \partial_{\mu\nu} \Omega^{ijk} = 1/x_{ijk}^{\mu\nu} \eta_{\mu\nu}^{ijk} \sigma^{ijk} + A_{\mu\nu} \\ &= 1/x^{ijk} + \rho^{ijk} \eta_{\mu\nu}^{ijk} x^{\mu\nu} \sigma^{ijk} + F_{\mu\nu} = 2\rho^{ijk} / (x^{ijk} + \rho^{ijk}) \exp^{ijk} \eta_{\mu\nu}^{ijk} \sigma^{ijk} \end{aligned}$$

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$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\Omega(x) = x_\mu\sigma^\mu/\sqrt{x_\mu^i} + A_\mu \mapsto i\Omega\partial_\mu\Omega^{ikj} = 1/x_{ikj}^\mu\eta_{\mu v}^i\sigma^i + A_\mu \\ &= 1/x^{ikj} + \rho^{ikj}\eta_{\mu v}^i x^v\sigma^i + F_{\mu v} = 2\rho^{ikj}/(x^{ikj} + \rho^{ikj})\exp^{ikj}\eta_{\mu v}^i\sigma^i\end{aligned}$$

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$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \Omega(x) = x_\nu \sigma^\nu / \sqrt{x_\nu^i + A_\nu} \mapsto i\Omega \partial_\nu \Omega^{ikj} = 1/x_{ikj}^\nu \eta_{\nu\mu}^i \sigma^i + A_\nu$$

$$= 1/x^{ikj} + \rho^{ikj} \eta_{\nu\mu}^i x^\mu \sigma^i + F_{\nu\mu} = 2\rho^{ikj} / (x^{ikj} + \rho^{ikj}) \exp^{ikj} \eta_{\nu\mu}^i \sigma^i$$

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$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\Omega(x) = x_{v\mu}\sigma^{v\mu}/\sqrt{x_{v\mu}^{ikj}} + A_{v\mu} \mapsto ikj\Omega\partial_{v\mu}\Omega^{ikj} = 1/x_{ikj}^{v\mu}\eta_{v\mu}^{ikj}\sigma^{ikj} + A_{v\mu} \\ &= 1/x^{ikj} + \rho^{ikj}\eta_{v\mu}^{ikj}x^{v\mu}\sigma^{ikj} + F_{v\mu} = 2\rho^{ikj}/(x^{ikj} + \rho^{ikj})\exp^{ikj}\eta_{v\mu}^{ikj}\sigma^{ikj}\end{aligned}$$

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$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\Omega(x) = x_v\sigma^v/\sqrt{x_v^j} + A_v \mapsto j\Omega\partial_v\Omega^{jik} = 1/x_{jik}^v\eta_{v\mu}^j\sigma^j + A_v \\ &= 1/x^{jik} + \rho^{jik}\eta_{v\mu}^j x^\mu\sigma^j + F_{v\mu} = 2\rho^{jik}/(x^{jik} + \rho^{jik})\exp^{jik}\eta_{v\mu}^j\sigma^j\end{aligned}$$

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$$\eta_{vj}^1 = \begin{matrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{matrix} \quad \eta_{vj}^2 = \begin{matrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ -1 & 0 & 0 \end{matrix} \quad \eta_{vj}^3 = \begin{matrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{matrix} \quad \eta_{vj}^\infty = \begin{matrix} 0 & 1 & 0 \\ 0 & 1 & 1 \\ -1 & 0 & 0 \end{matrix}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\Omega(x) = x_{\mu\nu}\sigma^{\mu\nu}/\sqrt{x_{\mu\nu}^{jik}} + A_{\mu\nu} \mapsto jik\Omega\partial_{\mu\nu}\Omega^{jik} = 1/x_{jik}^{\mu\nu}\eta_{\mu\nu}^{jik}\sigma^{jik} + A_{\mu\nu} \\ &= 1/x^{jik} + \rho^{jik}\eta_{\mu\nu}^{jik} x^{\mu\nu}\sigma^{jik} + F_{\mu\nu} = 2\rho^{jik}/(x^{jik} + \rho^{jik})\exp^{jik}\eta_{\mu\nu}^{jik}\sigma^{jik}\end{aligned}$$

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$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\Omega(x) = x_{v\mu}\sigma^{v\mu}/\sqrt{x_{v\mu}^{jik}} + A_{v\mu} \mapsto jik\Omega\partial_{v\mu}\Omega^{jik} = 1/x_{jik}^{v\mu}\eta_{v\mu}^{jik}\sigma^{jik} + A_{v\mu} \\ &= 1/x^{jik} + \rho^{jik}\eta_{v\mu}^{jik}x^{v\mu}\sigma^{jik} + F_{v\mu} = 2\rho^{jik}/(x^{jik} + \rho^{jik})\exp^{jik}\eta_{v\mu}^{jik}\sigma^{jik}\end{aligned}$$

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$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\Omega(x) = x_{v\mu}\sigma^{v\mu}/\sqrt{x_{v\mu}^{jki}} + A_{v\mu} \mapsto jki\Omega\partial_{v\mu}\Omega^{jki} = 1/x_{jki}^{v\mu}\eta_{v\mu}^{jki}\sigma^{jki} + A_{v\mu} \\ &= 1/x^{jki} + \rho^{jki}\eta_{v\mu}^{jki}x^{v\mu}\sigma^{jki} + F_{v\mu} = 2\rho^{jki}/(x^{jki} + \rho^{jki})\exp^{jki}\eta_{v\mu}^{jki}\sigma^{jki}\end{aligned}$$

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$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\Omega(x) = x_v\sigma^v/\sqrt{x_v^k} + A_v \mapsto k\Omega\partial_v\Omega^{kij} = 1/x_{kij}^v\eta_{v\mu}^k\sigma^k + A_v \\ &= 1/x^{kij} + \rho^{kij}\eta_{v\mu}^k x^\mu\sigma^k + F_{v\mu} = 2\rho^{kij}/(x^{kij} + \rho^{kij})\exp^{kij}\eta_{v\mu}^k\sigma^k\end{aligned}$$

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$$\eta_{vk}^1 = \begin{matrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{matrix} \quad \eta_{vk}^2 = \begin{matrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ -1 & 0 & 0 \end{matrix} \quad \eta_{vk}^3 = \begin{matrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{matrix} \quad \eta_{vk}^\infty = \begin{matrix} 0 & 1 & 0 \\ 0 & 1 & 1 \\ -1 & 0 & 0 \end{matrix}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\Omega(x) = x_{\mu\nu}\sigma^{\mu\nu}/\sqrt{x_{\mu\nu}^{kij}} + A_{\mu\nu} \mapsto kij\Omega\partial_{\mu\nu}\Omega^{kij} = 1/x_{kij}^{\mu\nu}\eta_{\mu\nu}^{kij}\sigma^{kij} + A_{\mu\nu} \\ &= 1/x^{kij} + \rho^{kij}\eta_{\mu\nu}^{kij} x^{\mu\nu}\sigma^{kij} + F_{\mu\nu} = 2\rho^{kij}/(x^{kij} + \rho^{kij})\exp^{kij}\eta_{\mu\nu}^{kij}\sigma^{kij}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\Omega(y) = y_{\mu\nu}\sigma^{\mu\nu}/\sqrt{y_{\mu\nu}^{kij}} + A_{\mu\nu} \mapsto kij\Omega\partial_{\mu\nu}\Omega^{kij} = 1/y_{kij}^{\mu\nu}\eta_{\mu\nu}^{kij}\sigma^{kij} + A_{\mu\nu} \\ &= 1/y^{kij} + \rho^{kij}\eta_{\mu\nu}^{kij} y^{\mu\nu}\sigma^{kij} + F_{\mu\nu} = 2\rho^{kij}/(y^{kij} + \rho^{kij})\exp^{kij}\eta_{\mu\nu}^{kij}\sigma^{kij}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\Omega(z) = z_{\mu\nu}\sigma^{\mu\nu}/\sqrt{z_{\mu\nu}^{kij}} + A_{\mu\nu} \mapsto kij\Omega\partial_{\mu\nu}\Omega^{kij} = 1/z_{kij}^{\mu\nu}\eta_{\mu\nu}^{kij}\sigma^{kij} + A_{\mu\nu} \\ &= 1/z^{kij} + \rho^{kij}\eta_{\mu\nu}^{kij} z^{\mu\nu}\sigma^{kij} + F_{\mu\nu} = 2\rho^{kij}/(z^{kij} + \rho^{kij})\exp^{kij}\eta_{\mu\nu}^{kij}\sigma^{kij}\end{aligned}$$

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$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\Omega(x) = x_{v\mu}\sigma^{v\mu}/\sqrt{x_{v\mu}^{kij}} + A_{v\mu} \mapsto kij\Omega\partial_{v\mu}\Omega^{kij} = 1/x_{kij}^{v\mu}\eta_{v\mu}^{kij}\sigma^{kij} + A_{v\mu} \\ &= 1/x^{kij} + \rho^{kij}\eta_{v\mu}^{kij}x^{v\mu}\sigma^{kij} + F_{v\mu} = 2\rho^{kij}/(x^{kij} + \rho^{kij})\exp^{kij}\eta_{v\mu}^{kij}\sigma^{kij}\end{aligned}$$

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$$\eta_{v\mu k}^1 = \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ 1 & 0 & 0 \end{pmatrix} \quad \eta_{v\mu k}^2 = \begin{pmatrix} 0 & -1 & 0 \\ 0 & 0 & 1 \\ -1 & 0 & 0 \end{pmatrix} \quad \eta_{v\mu k}^3 = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 0 & -1 \\ 1 & 0 & 0 \end{pmatrix} \quad \eta_{v\mu k}^\infty = \begin{pmatrix} 0 & 1 & 0 \\ 0 & 1 & 1 \\ -1 & 0 & 0 \end{pmatrix}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\Omega(x) = x_\mu\sigma^\mu/\sqrt{x_\mu^k} + A_\mu \mapsto k\Omega\partial_\mu\Omega^{kji} = 1/x_{kji}^\mu\eta_{\mu v}^k\sigma^k + A_\mu \\ &= 1/x^{kji} + \rho^{kji}\eta_{\mu v}^kx^v\sigma^k + F_{\mu v} = 2\rho^{kji}/(x^{kji} + \rho^{kji})\exp^{kji}\eta_{\mu v}^k\sigma^k\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\Omega(y) = y_\mu\sigma^\mu/\sqrt{y_\mu^k} + A_\mu \mapsto k\Omega\partial_\mu\Omega^{kji} = 1/y_{kji}^\mu\eta_{\mu v}^k\sigma^k + A_\mu \\ &= 1/y^{kji} + \rho^{kji}\eta_{\mu v}^ky^v\sigma^k + F_{\mu v} = 2\rho^{kji}/(y^{kji} + \rho^{kji})\exp^{kji}\eta_{\mu v}^k\sigma^k\end{aligned}$$

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$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\Omega(x) = x_v\sigma^v/\sqrt{x_v^k} + A_v \mapsto k\Omega\partial_v\Omega^{kji} = 1/x_{kji}^v\eta_{v\mu}^k\sigma^k + A_v \\ &= 1/x^{kji} + \rho^{kji}\eta_{v\mu}^k x^\mu\sigma^k + F_{v\mu} = 2\rho^{kji}/(x^{kji} + \rho^{kji})\exp^{kji}\eta_{v\mu}^k\sigma^k\end{aligned}$$

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$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle V(x) = \lambda(x_{\mu\nu\rho\sigma}^{ijk} + a_{\mu\nu\rho\sigma}^{ijk})\exp_{\mu\nu\rho\sigma}^{ijk} \frac{\partial\theta}{\xi\mathbb{R}^4} = \delta\varphi\phi\phi\phi d\omega(\tau) \\ &= a \tanh/\cosh + \sinh(w/\pi^2(\tau - \tau_{\mu\nu\rho\sigma}^{ijk}))\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle V(x) = \lambda(x_{ijk}^{\mu\nu\rho\sigma} + a_{ijk}^{\mu\nu\rho\sigma})\exp_{ijk}^{\mu\nu\rho\sigma} \frac{\partial\theta}{\xi\mathbb{R}^4} = \delta\varphi\phi\phi\phi d\omega(\tau) \\ &= a \tanh/\cosh + \sinh(w/\pi^2(\tau - \tau_{ijk}^{\mu\nu\rho\sigma}))\end{aligned}$$

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$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \langle a | e^{-HT} | -a \rangle = N \int_{x(0)=-a}^{x(T)=+a} Dx(\tau) e^{S_E[x(\tau)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle a | e^{+HT} | +a \rangle \\ &= N \int_{x(T)=+a}^{x(0)=-a} Dx(\tau) e^{S_E[x(\tau)]} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \langle b | e^{-HT} | -b \rangle = N \int_{x(0)=-b}^{x(T)=+b} Dx(\tau) e^{S_E[x(\tau)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle b | e^{+HT} | +b \rangle \\ &= N \int_{x(T)=+b}^{x(0)=-b} Dx(\tau) e^{S_E[x(\tau)]} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \langle c | e^{-HT} | -c \rangle = N \int_{x(0)=-c}^{x(T)=+c} Dx(\tau) e^{S_E[x(\tau)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle c | e^{+HT} | +c \rangle \\ &= N \int_{x(T)=+c}^{x(0)=-c} Dx(\tau) e^{S_E[x(\tau)]} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \langle a | e^{-HT} | -a \rangle = N \int_{y(0)=-a}^{y(T)=+a} Dy(\tau) e^{S_E[y(\tau)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle a | e^{+HT} | +a \rangle \\ &= N \int_{y(T)=+a}^{y(0)=-a} Dy(\tau) e^{S_E[y(\tau)]} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \langle b | e^{-HT} | -b \rangle = N \int_{y(0)=-b}^{y(T)=+b} Dy(\tau) e^{S_E[y(\tau)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle b | e^{+HT} | +b \rangle \\ &= N \int_{y(T)=+b}^{y(0)=-b} Dy(\tau) e^{S_E[y(\tau)]} \end{aligned}$$

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$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \langle a | e^{-HT} | -a \rangle = N \int_{z(0)=-a}^{z(T)=+a} Dz(\tau) e^{S_E[z(\tau)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle a | e^{+HT} | +a \rangle \\ &= N \int_{z(T)=+a}^{z(0)=-a} Dz(\tau) e^{S_E[z(\tau)]} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \langle b | e^{-HT} | -b \rangle = N \int_{z(0)=-b}^{z(T)=+b} Dz(\tau) e^{S_E[z(\tau)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle b | e^{+HT} | +b \rangle \\ &= N \int_{z(T)=+b}^{z(0)=-b} Dz(\tau) e^{S_E[z(\tau)]} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \langle c | e^{-HT} | -c \rangle = N \int_{z(0)=-c}^{z(T)=+c} Dz(\tau) e^{S_E[z(\tau)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle c | e^{+HT} | +c \rangle \\ &= N \int_{z(T)=+c}^{z(0)=-c} Dz(\tau) e^{S_E[z(\tau)]} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \langle a | e^{-HT} | -a \rangle = N \int_{x(0)=-a}^{x(T)=+a} Dx(\mu\nu\rho\sigma) e^{S_E[x(\mu\nu\rho\sigma)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle a | e^{+HT} \\ &| +a \rangle = N \int_{x(T)=+a}^{x(0)=-a} Dx(\mu\nu\rho\sigma) e^{S_E[x(\mu\nu\rho\sigma)]} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \langle b | e^{-HT} | -b \rangle = N \int_{x(0)=-b}^{x(T)=+b} Dx(\mu\nu\rho\sigma) e^{S_E[x(\mu\nu\rho\sigma)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle b | e^{+HT} \\ &| +b \rangle = N \int_{x(T)=+b}^{x(0)=-b} Dx(\mu\nu\rho\sigma) e^{S_E[x(\mu\nu\rho\sigma)]} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \langle c | e^{-HT} | -c \rangle = N \int_{x(0)=-c}^{x(T)=+c} Dx(\mu\nu\rho\sigma) e^{S_E[x(\mu\nu\rho\sigma)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle c | e^{+HT} | +c \rangle \\ &= N \int_{x(T)=+c}^{x(0)=-c} Dx(\mu\nu\rho\sigma) e^{S_E[x(\mu\nu\rho\sigma)]} \end{aligned}$$



$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle a | e^{-HT} | -a \rangle = N \int_{y(0)=-a}^{y(T)=+a} Dy(\mu\nu\rho\sigma) e^{S_E[y(\mu\nu\rho\sigma)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle a | e^{+HT} | +a \rangle = N \int_{y(T)=+a}^{y(0)=-a} Dy(\mu\nu\rho\sigma) e^{S_E[y(\mu\nu\rho\sigma)]}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle b | e^{-HT} | -b \rangle = N \int_{y(0)=-b}^{y(T)=+b} Dy(\mu\nu\rho\sigma) e^{S_E[y(\mu\nu\rho\sigma)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle b | e^{+HT} | +b \rangle = N \int_{y(T)=+b}^{y(0)=-b} Dy(\mu\nu\rho\sigma) e^{S_E[y(\mu\nu\rho\sigma)]}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle c | e^{-HT} | -c \rangle = N \int_{y(0)=-c}^{y(T)=+c} Dy(\mu\nu\rho\sigma) e^{S_E[y(\mu\nu\rho\sigma)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle c | e^{+HT} | +c \rangle = N \int_{y(T)=+c}^{y(0)=-c} Dy(\mu\nu\rho\sigma) e^{S_E[y(\mu\nu\rho\sigma)]}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle a | e^{-HT} | -a \rangle = N \int_{z(0)=-a}^{z(T)=+a} Dz(\mu\nu\rho\sigma) e^{S_E[z(\mu\nu\rho\sigma)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle a | e^{+HT} | +a \rangle = N \int_{z(T)=+a}^{z(0)=-a} Dz(\mu\nu\rho\sigma) e^{S_E[z(\mu\nu\rho\sigma)]}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle b | e^{-HT} | -b \rangle = N \int_{z(0)=-b}^{z(T)=+b} Dz(\mu\nu\rho\sigma) e^{S_E[z(\mu\nu\rho\sigma)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle b | e^{+HT} | +b \rangle = N \int_{z(T)=+b}^{z(0)=-b} Dz(\mu\nu\rho\sigma) e^{S_E[z(\mu\nu\rho\sigma)]}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle c | e^{-HT} | -c \rangle = N \int_{z(0)=-c}^{z(T)=+c} Dz(\mu\nu\rho\sigma) e^{S_E[z(\mu\nu\rho\sigma)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle c | e^{+HT} | +c \rangle = N \int_{z(T)=+c}^{z(0)=-c} Dz(\mu\nu\rho\sigma) e^{S_E[z(\mu\nu\rho\sigma)]}$$



$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\langle a|e^{-HT}| -a\rangle = N \int_{x(0)=-a}^{x(T)=+a} Dx(ijk) e^{SE[x(ijk)]} + \hat{H}|\psi\rangle = E_\psi|\psi\rangle\langle a|e^{+HT}| +a\rangle \\ &= N \int_{x(T)=+a}^{x(0)=-a} Dx(ijk) e^{SE[x(ijk)]}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\langle b|e^{-HT}| -b\rangle = N \int_{x(0)=-b}^{x(T)=+b} Dx(ijk) e^{SE[x(ijk)]} + \hat{H}|\psi\rangle = E_\psi|\psi\rangle\langle b|e^{+HT}| +b\rangle \\ &= N \int_{x(T)=+b}^{x(0)=-b} Dx(ijk) e^{SE[x(ijk)]}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\langle c|e^{-HT}| -c\rangle = N \int_{x(0)=-c}^{x(T)=+c} Dx(ijk) e^{SE[x(ijk)]} + \hat{H}|\psi\rangle = E_\psi|\psi\rangle\langle c|e^{+HT}| +c\rangle \\ &= N \int_{x(T)=+c}^{x(0)=-c} Dx(ijk) e^{SE[x(ijk)]}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\langle a|e^{-HT}| -a\rangle = N \int_{y(0)=-a}^{y(T)=+a} Dy(ijk) e^{SE[y(ijk)]} + \hat{H}|\psi\rangle = E_\psi|\psi\rangle\langle a|e^{+HT}| +a\rangle \\ &= N \int_{y(T)=+a}^{y(0)=-a} Dy(ijk) e^{SE[y(ijk)]}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\langle b|e^{-HT}| -b\rangle = N \int_{y(0)=-b}^{y(T)=+b} Dy(ijk) e^{SE[y(ijk)]} + \hat{H}|\psi\rangle = E_\psi|\psi\rangle\langle b|e^{+HT}| +b\rangle \\ &= N \int_{y(T)=+b}^{y(0)=-b} Dy(ijk) e^{SE[y(ijk)]}\end{aligned}$$

$$\begin{aligned}\hat{H}|\psi\rangle &= E_\psi|\psi\rangle\langle c|e^{-HT}| -c\rangle = N \int_{y(0)=-c}^{y(T)=+c} Dy(ijk) e^{SE[y(ijk)]} + \hat{H}|\psi\rangle = E_\psi|\psi\rangle\langle c|e^{+HT}| +c\rangle \\ &= N \int_{y(T)=+c}^{y(0)=-c} Dy(ijk) e^{SE[y(ijk)]}\end{aligned}$$



$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \langle a | e^{-HT} | -a \rangle = N \int_{z(0)=-a}^{z(T)=+a} Dz(ijk) e^{S_E[z(ijk)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle a | e^{+HT} | +a \rangle \\ &= N \int_{z(T)=+a}^{z(0)=-a} Dz(ijk) e^{S_E[z(ijk)]} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \langle b | e^{-HT} | -b \rangle = N \int_{z(0)=-b}^{z(T)=+b} Dz(ijk) e^{S_E[z(ijk)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle b | e^{+HT} | +b \rangle \\ &= N \int_{z(T)=+b}^{z(0)=-b} Dz(ijk) e^{S_E[z(ijk)]} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle \langle c | e^{-HT} | -c \rangle = N \int_{z(0)=-c}^{z(T)=+c} Dz(ijk) e^{S_E[z(ijk)]} + \hat{H} | \psi \rangle = E_\psi | \psi \rangle \langle c | e^{+HT} | +c \rangle \\ &= N \int_{z(T)=+c}^{z(0)=-c} Dz(ijk) e^{S_E[z(ijk)]} \end{aligned}$$

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle x(\tau) = \kappa(\tau) + \delta x(\tau) = \hat{H} | \psi \rangle = E_\psi | \psi \rangle S_E[x(\tau)] \\ &= S_{instanton} \\ &+ \int_{ijk} d(\tau) \delta(\tau) \partial(\tau) \Omega(\tau) \varphi(\tau) \phi(\tau) \xi(\tau) \lambda(\tau) \frac{\omega}{p} \cdot \mathbb{R}^4 / x^n \int_{x(0)=-a}^{x(T)=+a} D\infty(\tau) e^{-S_E[x(\tau)]} \\ &= e^{-S_{instanton}} \int_{\delta x(0)=0}^{\delta x(T)=0} D\delta(\tau) e^{d(\tau) \delta(\tau) \partial(\tau) \Omega(\tau) \varphi(\tau) \phi(\tau) \xi(\tau) \lambda(\tau) \frac{\omega}{p} \cdot \frac{\mathbb{R}^4}{x^n}} \\ &\approx e^{-S_{instanton}} / d\omega_{\lambda\nu/\lambda\sigma}^{\lambda\mu/\lambda\rho} \Delta \nabla \Omega \eta \varphi \phi \end{aligned}$$

r. Análisis de Campos Yang – Mills (Teorización Final).

$$\begin{aligned} \hat{H} | \psi \rangle &= E_\psi | \psi \rangle S_{YM} + S_{gf\mu\nu} \int_{ijk=m}^{ijk=n} \lambda 1/g^{\mu\nu\rho\sigma} \int_v^\mu d_\varphi^\omega \theta \Omega \text{tr} \left[\frac{1}{2} \dot{F}_{\mu\nu} \dot{F}^{\mu\nu} + n \dot{F}^{\mu\nu} \dot{D}_\mu \lambda \partial / \Delta \nabla \delta A_\nu \right. \\ &+ \dot{D}^\mu \lambda \partial / \Delta \nabla \delta A^\nu \dot{D}_\mu \lambda \partial / \Delta \nabla \delta A_\nu - \dot{D}^\mu \lambda \partial / \Delta \nabla \delta A^\nu \dot{D}_\nu \lambda \partial / \Delta \nabla \delta A_\mu - i \dot{F}^{\mu\nu} \dot{F}_{\mu\nu} [\delta A_\mu, \delta A_\nu] \\ &\left. - 2ijk \dot{D}^\mu \lambda \partial / \Delta \nabla \delta A^\nu [\delta A_\mu, \delta A_\nu] - 1/2 [\delta A^\mu, \delta A^\nu] [\delta A_\mu, \delta A_\nu] \right] \end{aligned}$$



$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle \det(\partial G(\check{A}^\omega, \delta A^\omega) / \partial \omega) \\ = \oint_{\mu}^v Dc Dc^\dagger \exp(-1/g^{v\mu} \oint_{\mu}^v d^{v\mu} \text{tr}[-e^\dagger (\dot{D}^{v\mu\rho\sigma} c + ijkc^\dagger [(\dot{D}^{v\mu\rho\sigma} \delta A_{v\mu\rho\sigma}, c)])])$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle 1/g^{\mu\nu} \oint_{\nu}^{\mu} d^{\mu\nu} n \text{tr}[1/2 \dot{F}_{\mu\nu} \dot{F}^{\mu\nu} + n \dot{F}^{\mu\nu} \dot{D}_\mu \delta A_\nu + \dot{D}^\mu \delta A^\nu \dot{D}_\mu \delta A_\nu - nijk \dot{F}^{\mu\nu} [\delta A_\mu, \delta A_\nu] \\ + \dot{D}_\mu c^\dagger \dot{D}^\mu c - nijk \dot{D}^\mu \delta A^\nu [\delta A_\mu, \delta A_\nu] - 1/2 [\delta A^\mu, \delta A^\nu] [\delta A_\mu, \delta A_\nu] + ic^\dagger [\dot{D}^\mu \delta A_\mu, c]]$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle 1/g^{v\mu} \oint_{\mu}^v d^{v\mu} n \text{tr}[1/2 \dot{F}_{v\mu} \dot{F}^{v\mu} + n \dot{F}^{v\mu} \dot{D}_\nu \delta A_\mu + \dot{D}^\nu \delta A^\mu \dot{D}_\nu \delta A_\mu - nijk \dot{F}^{v\mu} [\delta A_\nu, \delta A_\mu] \\ + \dot{D}_\nu c^\dagger \dot{D}^\nu c - nijk \dot{D}^\nu \delta A^\mu [\delta A_\nu, \delta A_\mu] - 1/2 [\delta A^\nu, \delta A^\mu] [\delta A_\nu, \delta A_\mu] + ic^\dagger [\dot{D}^\nu \delta A_\nu, c]]$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle e^{-S_{eff}[\check{A}, \delta, A, c]} = \oint_{\nu}^{\mu} D\delta A Dc Dc^\dagger e^{-S[\check{A}, \delta, A, c]} = e^{-S_{eff}[\check{A}]} \\ = \det^m \Delta_{gauge} \nabla_{gauge} \det^n \Delta_{ghost} \nabla_{ghost} e^{\frac{1}{2g^{\check{A}, \delta, A, c} \oint_{\nu}^{\mu} d_{\nu}^{\mu} n \text{tr} \dot{F}_{\mu\nu} \dot{F}^{\mu\nu}}} = \Delta_{gauge}^{\mu\nu} \Delta_{gauge}^{\mu\nu} \nabla \\ = \dot{D}^{\mu\nu} \delta^{\mu\nu} + 2ijk [\dot{F}^{\mu\nu} \Delta_{ghost}^{\mu\nu} \nabla - c^\dagger = S_{eff}[\check{A}, \delta, A, c] \\ = 1/2 g_{\nu}^{\mu} \oint_{\nu}^{\mu} d_{\nu}^{\mu} n \text{tr} \dot{F}_{\mu\nu} \dot{F}^{\mu\nu} + 1/2 \text{Tr} \log \Delta_{gauge}^{\mu\nu} \Delta_{gauge}^{\mu\nu} \nabla - \text{Tr} \log \Delta_{ghost}^{\mu\nu} \Delta_{ghost}^{\mu\nu} \nabla \\ = \xi_{\lambda\Omega\psi}^{\sigma\zeta} \sum \int \int \int \int \hbar \phi \text{B} \check{X} \check{X} \check{X} \check{X} \psi \check{X} \check{X} \zeta \pi m c^{\mathbb{R}^4}$$

$$\hat{H} | \psi \rangle = E_\psi | \psi \rangle e^{-S_{eff}[\check{A}, \delta, A, c]} = \oint_{\mu}^v D\delta A Dc Dc^\dagger e^{-S[\check{A}, \delta, A, c]} = e^{-S_{eff}[\check{A}]} \\ = \det^m \Delta_{gauge} \nabla_{gauge} \det^n \Delta_{ghost} \nabla_{ghost} e^{\frac{1}{2g^{\check{A}, \delta, A, c} \oint_{\mu}^v d_{\mu}^v n \text{tr} \dot{F}_{\nu\mu} \dot{F}^{v\mu}}} = \Delta_{gauge}^{v\mu} \Delta_{gauge}^{v\mu} \nabla \\ = \dot{D}^{v\mu} \delta^{v\mu} + 2ijk [\dot{F}^{v\mu} \Delta_{ghost}^{v\mu} \nabla - c^\dagger = S_{eff}[\check{A}, \delta, A, c] \\ = 1/2 g_{\mu}^v \oint_{\mu}^v d_{\mu}^v n \text{tr} \dot{F}_{\nu\mu} \dot{F}^{v\mu} + 1/2 \text{Tr} \log \Delta_{gauge}^{v\mu} \Delta_{gauge}^{v\mu} \nabla - \text{Tr} \log \Delta_{ghost}^{v\mu} \Delta_{ghost}^{v\mu} \nabla \\ = \xi_{\lambda\Omega\psi}^{\sigma\zeta} \sum \int \int \int \int \hbar \phi \text{B} \check{X} \check{X} \check{X} \check{X} \psi \check{X} \check{X} \zeta \pi m c^{\mathbb{R}^4}$$



$$\begin{aligned}
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle S_{quad} = 1/2 g_v^\mu \oint_\mu^v d_\mu^v n \operatorname{tr} (\partial_v \check{A}_\mu \partial^v \check{A}^\mu - \partial_v \check{A}^\mu \partial_\mu \check{A}^v) \\
&= 1/2 g^{v\mu} \oint_\mu^v d^{v\mu} k / (n\pi^{v\mu}) \operatorname{tr} [\check{A}_v(k) \check{A}_\mu(-k)] (k^v k^\mu - k_v k_\mu + k_\mu^v \delta_\mu^v) \\
&= \operatorname{Tr} \log \Delta_{ghost\ ghost}^{v\mu} \nabla \\
&= C(adj)/8\pi^2 (16\pi^2) \oint_\mu^v d_\mu^v k_\rho^\sigma \delta\Omega \lambda^\dagger / 8\pi^2 \operatorname{tr} [\check{A}_v(k) \check{A}_\mu(-k)] (k^v k^\mu - k_v k_\mu + k_\mu^v \delta_\mu^v) \\
&= \log \Lambda_{UV}^{v\mu} / k_\rho^\sigma \lambda \Omega \phi \xi \delta \phi \eta c^\dagger \theta
\end{aligned}$$

$$\begin{aligned}
\hat{H} | \psi \rangle &= E_\psi | \psi \rangle \Delta \nabla_{gauge}^{\mu\nu} = \Delta \nabla_{ghost}^{\mu\nu} \partial \delta_{v\rho}^{\mu\sigma} + nijk [\dot{F}^{\mu\nu}, \infty] = \operatorname{Tr} \log \Delta \nabla_{gauge}^{\mu\nu} \\
&= 16 \operatorname{Tr} \log \Delta \nabla_{ghost}^{\mu\nu} + \dot{F}_{\mu\nu} \text{ terms} \\
&= -1/2 (2ijk) \exp^{\mu\nu} \operatorname{Tr} ((-\partial^{\mu\nu}) \exp^{-\mu\nu} [\dot{F}_{\mu\nu}, [(-\partial^{\mu\nu}) \exp^{-\mu\nu} \dot{F}^{\mu\nu}, \infty]]) \\
&= 1/2 \iiint_v^\mu d_\mu^v k_\rho^\sigma / (16\pi^2) \operatorname{tr}_{adj} [\check{A}_\mu(k) \check{A}_v(-k)] \iiint_v^\mu d_\mu^v p_\rho^\sigma / (16\pi^2) - 16(k^\rho \delta^{\mu\sigma} \\
&\quad - k^\sigma \delta^{\mu\rho}) (k_\sigma \delta_\rho^v - k_\rho \delta_\sigma^v) / \rho^{\mu\nu} \sigma^{\mu\nu} (\rho_v^\mu + k_v^\mu) = \dot{F}_{\mu\nu} \text{ terms} \\
&= 16C(adj)/(32\pi^2) \iiint_v^\mu \frac{d^{\mu\nu} d_{\mu\nu} k_v^\mu}{16\pi^2} \operatorname{tr} [\check{A}_\mu(k) \check{A}_v(-k)] (k^\mu k^v - k_\mu k_v \\
&\quad + k_v^\mu \delta_v^\mu) \log \Lambda_{UV}^{\mu\nu} / k_\sigma^\rho \lambda \Omega \phi \xi \delta \phi \eta c^\dagger \theta = 1/2 \operatorname{Tr} \log \Delta \nabla_{gauge}^{\mu\nu} \\
&= 1/2 [16/4 - 8] C(adj)/16\pi^2 \oint_v^\mu d_\mu^v k_\rho^\sigma \delta\Omega \lambda^\dagger / 8\pi^2 \operatorname{tr} [\check{A}_\mu(k) \check{A}_v(-k)] (k^\mu k^v - k_\mu k_v \\
&\quad + k_v^\mu \delta_v^\mu) = \log \Lambda_{UV}^{\mu\nu} / k_\rho^\sigma \lambda \Omega \phi \xi \delta \phi \eta c^\dagger \theta
\end{aligned}$$



neutrones en núcleos), sin perder las premisas esenciales de la teoría de campos de Yang – Mills, esto es, por fuera de la teoría electrodébil de Glashow-Salam-Weinberg o la teoría del “campo de Higgs”.

Si bien es cierto, constituyese en una propiedad notable de la teoría cuántica de Yang-Mills, la nominada "*libertad asintótica*", la misma que, permite determinar, que a distancias cortas el campo muestra un comportamiento cuántico muy similar a su comportamiento clásico; sin embargo, a largas distancias, la teoría de Yang – Mills, como queda demostrado, también aplica a largas distancias en el campo.

Finalmente, queda demostrado concluyentemente, que: **(i)** en los campos de Yang – Mills, existe una "brecha de masa", es decir, $\Delta > \text{constante}$, por lo que, cada excitación del vacío tiene energía de al menos Δ ; **(ii)** en los campos de Yang – Mills, existe un confinamiento de quarks, partiendo de la premisa de que, los estados físicos de las partículas, como el protón, el neutrón y el pión, son invariantes; y, **(iii)** en los campos de Yang – Mills, existe una ruptura de simetría quiral, lo que significa que el vacío es potencialmente invariante bajo un cierto subgrupo de simetría completa que actúa sobre los campos de quarks.

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